

# Package ‘rankrate’

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<https://github.com/pearce790/rankrate/>

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AIBS	<i>Real peer review data set from the American Institute of Biological Sciences (AIBS)</i>
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## Description

This real data set includes 12 judges (reviewers) and 28 objects (proposals), and demonstrates the ability of the Mallows-Binomial model to combine ratings and rankings for the purpose of demarcating real grant proposals for a funding agency.

## Usage

AIBS

## Format

A list with three elements: (1) rankings, a 12 x 18 matrix of rankings with one row per judge; (2) ratings, a 12 x 18 matrix of ratings, with one row per judge and one column per object; and (3) M, a number indicating the maximum (worst) integer score.

## Source

Originally published in: Gallo, Stephen A.. "Grant Peer Review Scoring Data with Criteria Scores" (2023). [https://figshare.com/articles/dataset/Grant\\_Peer\\_Review\\_Scoring\\_Data\\_with\\_Criteria\\_Scores/12728087/1](https://figshare.com/articles/dataset/Grant_Peer_Review_Scoring_Data_with_Criteria_Scores/12728087/1).

Originally analyzed in: Gallo, Stephen A., et al. "A new approach to peer review assessments: Score, then rank" (2023). *Research Integrity and Peer Review* 8:10 (10). <https://researchintegrityjournal.biomedcentral.com/articles/10.1186/s41073-023-00131-7>.

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ASTAR	<i>Calculate the exact MLE of a Mallows-Binomial distribution using an A* algorithm</i>
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---

### Description

This function estimates the exact MLE of a Mallows-Binomial distribution using an A\* tree search algorithm proposed in Pearce and Erosheva (2022). Algorithm may be very slow when number of objects exceeds 15, but is often still tractable for larger J when consensus is strong.

### Usage

```
ASTAR(rankings, ratings, M, keep_nodes = FALSE)
```

### Arguments

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
ratings	A matrix of ratings, one row per judge and one column per object.
M	Numeric specifying maximum (=worst quality) integer rating.
keep_nodes	Boolean specifying if function should retain the list of open nodes traversed during A* tree search. Defaults to FALSE.

### Value

A list with elements  $\pi_0$ , the estimated consensus ranking MLE,  $\rho$ , the estimated object quality parameter MLE,  $\theta$ , the estimated scale parameter MLE, and `numnodes`, number of nodes traversed during algorithm and a measure of computational complexity. If `keep_nodes == TRUE`, then the list also contains `nodes`, a matrix of open nodes remaining at the end of search. If multiple MLEs are found,  $\pi_0$ ,  $\rho$ , and  $\theta$  are returned a matrix elements, with one row per MLE.

### Examples

```
data("ToyData1")
ASTAR(ToyData1$rankings, ToyData1$ratings, ToyData1$M, keep_nodes=TRUE)
```

---

ci\_mb

*Bootstrap Confidence Intervals for Mallows-Binomial parameters.*


---

### Description

This function calculates confidence intervals for parameters in a Mallows-Binomial model using the nonparametric bootstrap.

### Usage

```
ci_mb(
  rankings,
  ratings,
  M,
  interval = 0.9,
  nsamples = 50,
  all = FALSE,
  method = "ASTAR"
)
```

### Arguments

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
ratings	A matrix of ratings, one row per judge and one column per object.
M	Numeric specifying maximum (=worst quality) integer rating.
interval	A numeric entry between 0 and 1 specifying the confidence interval (e.g., .90 indicates a 90% confidence interval). Defaults to 0.90.
nsamples	A numeric entry indicating desired number of bootstrap samples to be used when calculating confidence intervals. Defaults to 50.
all	A boolean indicating if estimated parameters from all bootstrap samples should be returned. Defaults to FALSE.
method	A character string indicating which estimation method to use when estimating parameters. Allowable options are currently "ASTAR", "Greedy", "GreedyLocal", and "FV". Defaults to exact search, "ASTAR".

### Value

A list with elements `ci`, a matrix of confidence intervals for Mallows-Binomial parameters, `ci_ranks`, a matrix of confidence intervals for object ranks, `bootstrap_pi0`, a matrix of bootstrap consensus rankings (returned only if `all==TRUE`), and `bootstrap_ptheta`, a matrix of bootstrap estimates of  $(p, \theta)$  (returned only if `all==TRUE`).

**Examples**

```
data("ToyData1")
ci_mb(ToyData1$rankings, ToyData1$ratings, ToyData1$M, method="ASTAR", all=TRUE)
```

---

dmall

---

*Calculate the density of rankings under a Mallows distribution*


---

**Description**

This function calculates the density of observation(s) under a Mallows distribution.

**Usage**

```
dmall(rankings, pi0, theta, log = FALSE)
```

**Arguments**

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
pi0	A vector specifying the consensus (modal probability) ranking; should be used only for tie-breaking equal values in p.
theta	A numeric entry specifying the Mallows scale parameter.
log	A boolean indicating if the log likelihood should be returned.

**Value**

A numeric value indicating the (log) likelihood of rankings under a Mallows distribution.

**Examples**

```
rankings1 <- matrix(c(1,2,3,3,1,2), nrow=2, byrow=TRUE)
rankings2 <- matrix(c(1,2,3,4,2,3,NA,NA), nrow=2, byrow=TRUE)
attr(rankings2, "assignments") <- matrix(c(rep(TRUE, 4), FALSE, TRUE, TRUE, TRUE), nrow=2, byrow=TRUE)
dmall(rankings=c(1,2,3,NA), pi0=c(1,2,3,4), theta=2)
dmall(rankings=rankings1, pi0=c(1,2,3), theta=2)
dmall(rankings=rankings2, pi0=c(1,2,3,4), theta=3, log=TRUE)
```

---

dmb	<i>Calculate the density of rankings and ratings under a Mallows-Binomial distribution.</i>
-----	---

---

### Description

This function calculates the density of observation(s) under a Mallows-Binomial distribution.

### Usage

```
dmb(rankings, ratings, p, theta, M, pi0 = NULL, log = FALSE)
```

### Arguments

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
ratings	A matrix of ratings, one row per judge and one column per object.
p	A vector specifying the underlying object qualities. All values between be between 0 and 1, inclusive.
theta	A numeric entry specifying the Mallows scale parameter.
M	Numeric specifying maximum (=worst quality) integer rating.
pi0	A vector specifying the consensus (modal probability) ranking; should be used only for tie-breaking equal values in p.
log	A boolean indicating if the log likelihood should be returned.

### Value

A numeric value indicating the (log) likelihood of rankings and ratings under a Mallows distribution.

### Examples

```
data(ToyData1)
dmb(rankings=ToyData1$rankings,ratings=ToyData1$ratings,p=c(.2,.5,.7),theta=1,M=ToyData1$M)
dmb(rankings=ToyData1$rankings,ratings=ToyData1$ratings,p=c(.25,.25,.7),theta=1,M=ToyData1$M,
pi0=c(1,2,3),log=TRUE)
```

---

fit_mb	<i>Calculate the exact or approximate MLE of a Mallows-Binomial distribution using various methods</i>
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---

## Description

This function calculates the exact or approximate MLE of a Mallows-Binomial distribution using a user-specified method.

## Usage

```
fit_mb(  
  rankings,  
  ratings,  
  M,  
  method = c("ASTAR", "Greedy", "GreedyLocal", "FV")  
)
```

## Arguments

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
ratings	A matrix of ratings, one row per judge and one column per object.
M	Numeric specifying maximum (=worst quality) integer rating.
method	A character string indicating which estimation method to use when estimating parameters. Allowable options are currently "ASTAR", "Greedy", "GreedyLocal", and "FV". Defaults to exact search, "ASTAR".

## Value

A list with elements  $\pi_0$ , the estimated consensus ranking MLE,  $p$ , the estimated object quality parameter MLE,  $\theta$ , the estimated scale parameter MLE, and  $\text{numnodes}$ , number of nodes traversed during algorithm and a measure of computational complexity. If multiple MLEs are found,  $\pi_0$ ,  $p$ , and  $\theta$  are returned a matrix elements, with one row per MLE.

## Examples

```
data("ToyData1")  
fit_mb(ToyData1$rankings, ToyData1$ratings, ToyData1$M, method="ASTAR")  
fit_mb(ToyData1$rankings, ToyData1$ratings, ToyData1$M, method="Greedy")  
fit_mb(ToyData1$rankings, ToyData1$ratings, ToyData1$M, method="GreedyLocal")  
fit_mb(ToyData1$rankings, ToyData1$ratings, ToyData1$M, method="FV")
```

---

FV	<i>Estimate the MLE of a Mallows-Binomial distribution using the FV method</i>
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---

**Description**

This function estimates the MLE of a Mallows-Binomial distribution using the FV method.

**Usage**

```
FV(rankings, ratings, M)
```

**Arguments**

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
ratings	A matrix of ratings, one row per judge and one column per object.
M	Numeric specifying maximum (=worst quality) integer rating.

**Value**

A list with elements  $\pi_0$ , the estimated consensus ranking MLE,  $\rho$ , the estimated object quality parameter MLE,  $\theta$ , the estimated scale parameter MLE, and `numnodes`, number of nodes traversed during algorithm and a measure of computational complexity. If multiple MLEs are found,  $\pi_0$ ,  $\rho$ , and  $\theta$  are returned a matrix elements, with one row per MLE.

**Examples**

```
data("ToyData1")
FV(ToyData1$rankings, ToyData1$ratings, ToyData1$M)
```

---

getQ	<i>Calculate Q Matrix</i>
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---

**Description**

This function calculates the Q matrix given a collection of (partial) rankings.

**Usage**

```
getQ(rankings, I, J)
```

**Arguments**

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
I	A numeric entry indicating the total number of judges providing rankings and ratings.
J	A numeric entry or vector of positive integers indicating total number of objects.

**Value**

A matrix with dimension  $J \times J$ .

**Examples**

```
rankings <- matrix(c(1,2,3,4,2,1,NA,NA),byrow=TRUE,nrow=2)
getQ(rankings=rankings,I=2,J=4)
attr(rankings,"assignments") <- matrix(c(rep(TRUE,7),FALSE),byrow=TRUE,nrow=2,ncol=4)
getQ(rankings=rankings,I=2,J=4)
```

---

Greedy	<i>Estimate the MLE of a Mallows-Binomial distribution using the Greedy method</i>
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---

**Description**

This function estimates the MLE of a Mallows-Binomial distribution using the Greedy method.

**Usage**

```
Greedy(rankings, ratings, M)
```

**Arguments**

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
ratings	A matrix of ratings, one row per judge and one column per object.
M	Numeric specifying maximum (=worst quality) integer rating.

**Value**

A list with elements  $\pi_0$ , the estimated consensus ranking MLE,  $p$ , the estimated object quality parameter MLE,  $\theta$ , the estimated scale parameter MLE, and  $\text{numnodes}$ , number of nodes traversed during algorithm and a measure of computational complexity. If multiple MLEs are found,  $\pi_0$ ,  $p$ , and  $\theta$  are returned a matrix elements, with one row per MLE.

**Examples**

```
data("ToyData1")
Greedy(ToyData1$rankings, ToyData1$ratings, ToyData1$M)
```

---

GreedyLocal	<i>Estimate the MLE of a Mallows-Binomial distribution using the "Greedy Local" method</i>
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---

**Description**

This function estimates the MLE of a Mallows-Binomial distribution using the GreedyLocal method, which is identical to the Greedy method but includes an automatic and targeted post-hoc local search.

**Usage**

```
GreedyLocal(rankings, ratings, M)
```

**Arguments**

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
ratings	A matrix of ratings, one row per judge and one column per object.
M	Numeric specifying maximum (=worst quality) integer rating.

**Value**

A list with elements  $\pi_0$ , the estimated consensus ranking MLE,  $\rho$ , the estimated object quality parameter MLE,  $\theta$ , the estimated scale parameter MLE, and numnodes, number of nodes traversed during algorithm and a measure of computational complexity. If multiple MLEs are found,  $\pi_0$ ,  $\rho$ , and  $\theta$  are returned a matrix elements, with one row per MLE.

**Examples**

```
data("ToyData1")
GreedyLocal(ToyData1$rankings, ToyData1$ratings, ToyData1$M)
```

---

kendall	<i>Calculate the Kendall's tau between rankings</i>
---------	---

---

**Description**

This function calculates Kendall's tau distance between ranking(s) and a central permutation,  $\pi_0$

**Usage**

```
kendall(rankings, pi0)
```

**Arguments**

rankings	A matrix of rankings, potentially with attribute "assignments" to signify separate reviewer assignments. One ranking per row.
pi0	A vector specifying the consensus (modal probability) ranking.

**Value**

A vector of the Kendall's tau distance between each ranking in rankings and  $\pi_0$ .

**Examples**

```
ranking1 <- c(2,1,3)
ranking2 <- matrix(c(2,1,3,1,2,3),byrow=TRUE,nrow=2)
ranking3 <- matrix(c(1,2,3,4,2,4,NA,NA),byrow=TRUE,nrow=2)
attr(ranking3,"assignments") <- matrix(c(TRUE,TRUE,TRUE,TRUE,
  FALSE,TRUE,FALSE,TRUE),byrow=TRUE,nrow=2)
kendall(ranking1,c(1,2,3))
kendall(ranking2,c(1,2,3))
kendall(ranking3,c(1,2,3,4))
```

---

psi	<i>Normalizing constant function of a Mallows distribution, psi</i>
-----	---

---

**Description**

This function calculates the normalizing constant of a Mallows distribution under the Kendall distance

**Usage**

```
psi(theta, J, R, log = FALSE)
```

**Arguments**

theta	A numeric entry specifying the Mallows scale parameter.
J	A numeric entry or vector of positive integers indicating total number of objects each judge has access to. If $\text{length}(J) > 1$ , R must be of same length or a single value.
R	A numeric entry or vector of positive integers indicating the length of the ranking provided by each judge. If $\text{length}(R) > 1$ , J must be of same length or a single value.
log	A boolean indicating if $\log(\text{psi})$ should be returned.

**Value**

A numeric value or vector representing normalizing constant of a Mallows distribution.

**Examples**

```
psi(theta=1, J=10, R=8)
psi(theta=2, J=c(4, 4, 3), R=c(2, 2, 1), log=TRUE)
```

---

 rmall

*Random Mallows generation.*


---

**Description**

This function randomly generates rankings from a Mallows distribution.

**Usage**

```
rmall(I, pi0, theta, R = NULL)
```

**Arguments**

I	A numeric entry indicating the number of observations to be drawn, i.e., the number of judges providing rankings and ratings.
pi0	A vector specifying the consensus (modal probability) ranking; should be used only for tie-breaking equal values in p.
theta	A numeric entry specifying the Mallows scale parameter.
R	A numeric entry specifying the length of the rankings to be drawn. When $R \leq \text{length}(p)$ , partial rankings are drawn by definition.

**Value**

A matrix of rankings (orderings) with one row per judge.

**Examples**

```
rmb(I=5,pi0=1:5,theta=1,R=3)
rmb(I=5,pi0=1:3,theta=.5,R=c(1,1,1,1,3))
rmb(I=5,pi0=1:3,theta=.5)
```

---

rmb	<i>Random Mallows-Binomial generation</i>
-----	---

---

**Description**

This function randomly generates rankings and ratings from a Mallows-Binomial distribution.

**Usage**

```
rmb(I, p, theta, M, pi0 = NULL, R = NULL)
```

**Arguments**

I	A numeric entry indicating the number of observations to be drawn, i.e., the number of judges providing rankings and ratings.
p	A vector specifying the underlying object qualities. All values between be between 0 and 1, inclusive.
theta	A numeric entry specifying the Mallows scale parameter.
M	A numeric entry specifying the maximum integer rating.
pi0	A vector specifying the consensus (modal probability) ranking; should be used only for tie-breaking equal values in p.
R	A numeric entry specifying the length of the rankings to be drawn. When $R \leq \text{length}(p)$ , partial rankings are drawn by definition.

**Value**

A list containing elements ratings, a matrix of integer ratings with one row per judge and one column per object, rankings, and matrix of rankings (orderings) with one row per judge, and M, the inputted maximum integer rating.

**Examples**

```
rmb(I=5,p=c(.1,.3,.4,.7,.9),theta=1,M=10)
rmb(I=10,p=c(.1,.3,.3,.7,.9),pi0=c(1,3,2,4,5),theta=5,M=40,R=3)
```

---

ToyData1	<i>Toy data set of rankings and ratings demonstrating tie-breaking</i>
----------	--

---

**Description**

This toy data set includes 16 judges and 3 objects, and demonstrates the ability of the Mallows-Binomial model to break ties in ratings via rankings.

**Usage**

ToyData1

**Format**

list with three elements: (1) rankings, a 16 x 3 matrix of rankings with one row per judge; (2) ratings, a 16 x 3 matrix of ratings, with one row per judge and one column per object; and (3) M, a number indicating the maximum (worst) integer score.

**Source**

Originally analyzed in: Gallo, Stephen A., et al. "A new approach to peer review assessments: Score, then rank" (2023). Research Integrity and Peer Review 8:10 (10). <https://researchintegrityjournal.biomedcentral.com/articles/10.1186/s41073-023-00131-7>.

---

ToyData2	<i>Toy data set of rankings and ratings demonstrating decision-making with partial rankings</i>
----------	---

---

**Description**

This toy data set includes 16 judges and 8 objects, and demonstrates the ability of the Mallows-Binomial model to estimate overall object orderings under partial rankings.

**Usage**

ToyData2

**Format**

list with three elements: (1) rankings, a 16 x 8 matrix of rankings with one row per judge; (2) ratings, a 16 x 8 matrix of ratings, with one row per judge and one column per object; and (3) M, a number indicating the maximum (worst) integer score.

**Source**

Originally analyzed in: Gallo, Stephen A., et al. "A new approach to peer review assessments: Score, then rank" (2023). Research Integrity and Peer Review 8:10 (10). <https://researchintegrityjournal.biomedcentral.com/articles/10.1186/s41073-023-00131-7>.

---

ToyData3	<i>Toy data set of rankings and ratings when judges express internally inconsistent preferences</i>
----------	---

---

### Description

This toy data set includes 16 judges and 3 objects, and demonstrates the ability of the Mallows-Binomial model to estimate overall object orderings even when judges provide sets of rankings and ratings which are internally inconsistent.

### Usage

```
ToyData3
```

### Format

list with three elements: (1) rankings, a 16 x 3 matrix of rankings with one row per judge; (2) ratings, a 16 x 3 matrix of ratings, with one row per judge and one column per object; and (3) M, a number indicating the maximum (worst) integer score.

### Source

Originally analyzed in: Gallo, Stephen A., et al. "A new approach to peer review assessments: Score, then rank" (2023). *Research Integrity and Peer Review* 8:10 (10). <https://researchintegrityjournal.biomedcentral.com/articles/10.1186/s41073-023-00131-7>.

---

to_rankings	<i>Convert ranks into rankings (orderings)</i>
-------------	--

---

### Description

This function converts a matrix of ranks into a matrix of rankings (i.e., orderings), potentially including reviewer assignments as an attribute of the ranking matrix. Additionally, it can be used to add an assignments matrix to an existing matrix of rankings.

### Usage

```
to_rankings(ranks, assignments = NULL, rankings = NULL)
```

**Arguments**

ranks	A matrix or vector of ranks, such that the (i,j) entry includes the rank given by judge i to proposal j. NA is used to indicate that no rank was assigned to a proposal, which may occur for two reasons: (1) If the assignments matrix is not specified or the (i,j) entry of assignments is TRUE, then an NA indicates that a proposal was considered worse than all ranked proposals. (2) If the (i,j) entry of assignments is FALSE, then NA indicates that a proposal was not considered by the judge and no information can be gleaned from the missing rank.
assignments	A matrix of booleans, such that the (i,j) entry is TRUE if judge i was assigned to review proposal j, and FALSE otherwise. If assignments is NULL, we assume all judges considered all proposals.
rankings	A matrix or vector of rankings. If a matrix, there should be one ranking per row.

**Value**

A matrix of rankings, with one row per ranking. If assignments argument is specified, then the rankings matrix will have the attribute "assignments".

**Examples**

```
ranks <- matrix(data=c(4,2,3,1,NA,1,2,3,NA,NA,1,NA),byrow=TRUE,nrow=3)
assignments=matrix(TRUE,byrow=TRUE,nrow=3,ncol=4)
to_rankings(ranks=ranks)
to_rankings(ranks=ranks,assignments=assignments)
to_rankings(assignments=matrix(TRUE,nrow=1,ncol=3),rankings=c(3,2,1))
```

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