

Package ‘ngme2’

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Type Package

Title Linear Latent Non-Gaussian Models with Flexible Distributions

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Description Fits and analyzes linear latent non-Gaussian models for temporal, spatial, and space-time data. The package provides model components for autoregressive and Ornstein-Uhlenbeck processes, random walks, Matern fields based on stochastic partial differential equations, separable and non-separable space-time models, graph-based Matern models, bivariate type-G fields, and user-defined sparse operators. Latent fields and observation models can use Gaussian and non-Gaussian noise distributions, including normal inverse Gaussian, generalized asymmetric Laplace, and skew-t distributions. Functions are included for simulation, likelihood-based estimation, prediction, cross-validation, convergence diagnostics, stochastic gradient optimization, batch-means confidence intervals, and posterior-like sampling. The modeling framework is described in Bolin, Jin, Simas and Wallin (2026) ``A Unified and Computationally Efficient Non-Gaussian Statistical Modeling Framework" <[doi:10.48550/arXiv.2602.23987](https://doi.org/10.48550/arXiv.2602.23987)>.

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<https://github.com/davidbolin/ngme2>

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BugReports <https://github.com/davidbolin/ngme2/issues>

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adagrad	<i>AdaGrad SGD optimization</i>
---------	---------------------------------

Description

AdaGrad SGD optimization

Usage

```
adagrad(stepsize = 0.05, epsilon = 1e-08)
```

Arguments

stepsize	stepsize for SGD
epsilon	epsilon for numerical stability

Details

The update rule for AdaGrad is:

$$v_t = v_{t-1} + g_t^2$$

$$x_{t+1} = x_t - \text{stepsize} * \frac{g_t}{\sqrt{v_t} + \epsilon}$$

Value

a list of control variables for optimization (used in `control_opt` function)

adam

Adam SGD optimization

Description

Adam SGD optimization

Usage

```
adam(stepsize = 0.05, beta1 = 0.9, beta2 = 0.999, epsilon = 1e-08)
```

Arguments

stepsize	stepsize for SGD
beta1	beta1 for Adam
beta2	beta2 for Adam
epsilon	epsilon for numerical stability

Details

The update rule for Adam is:

$$m_t = \beta_1 m_{t-1} + (1 - \beta_1) g_t$$

$$v_t = \beta_2 v_{t-1} + (1 - \beta_2) g_t^2$$

$$\hat{m}_t = m_t / (1 - \beta_1^t)$$

$$\hat{v}_t = v_t / (1 - \beta_2^t)$$

$$x_{t+1} = x_t - \text{stepsize} * \frac{\hat{m}_t}{\sqrt{\hat{v}_t + \epsilon}}$$

Value

a list of control variables for optimization (used in `control_opt` function)

adamW

*AdamW SGD optimization***Description**

AdamW SGD optimization

Usage

```
adamW(
  stepsize = 0.05,
  beta1 = 0.9,
  beta2 = 0.999,
  lambda = 0.01,
  epsilon = 1e-08
)
```

Arguments

stepsize	stepsize for SGD
beta1	beta1 for AdamW
beta2	beta2 for AdamW
lambda	lambda (weight decay) for AdamW
epsilon	epsilon for numerical stability

Details

The update rule for AdamW is:

$$m_t = \beta_1 m_{t-1} + (1 - \beta_1) g_t$$

$$v_t = \beta_2 v_{t-1} + (1 - \beta_2) g_t^2$$

$$\hat{m}_t = m_t / (1 - \beta_1^t)$$

$$\hat{v}_t = v_t / (1 - \beta_2^t)$$

$$x_{t+1} = x_t - \text{stepsize} * \left(\lambda x_t + \frac{\hat{m}_t}{\sqrt{\hat{v}_t + \epsilon}} \right)$$

Valuea list of control variables for optimization (used in `control_opt` function)

adaptive_gd	<i>Adaptive gradient descent</i>
-------------	----------------------------------

Description

Adaptive gradient descent optimizer.

Usage

```
adaptive_gd(stepsize = 0.01)
```

Arguments

stepsize	initial stepsize for SGD
----------	--------------------------

Details

Based on the method described in <https://arxiv.org/pdf/1910.09529>. The update rule for adaptive gradient descent is:

$$\lambda_k = \min(\sqrt{1 + \theta_{k-1}} \lambda_{k-1}, \frac{\|x_k - x_{k-1}\|}{2\|\nabla f(x_k) - \nabla f(x_{k-1})\|})$$

$$x_{k+1} = x_k - \lambda_k \nabla f(x_k)$$

$$\theta_k = \lambda_k / \lambda_{k-1}$$

Value

a list of control variables for optimization (used in `control_opt` function)

ar	<i>ngme AR(p) model specification</i>
----	---------------------------------------

Description

ngme AR(p) model specification

Usage

```
ar(mesh = NULL, rho = NULL, order = NULL)
```

Arguments

mesh	integer vector or <code>inla.mesh.1d</code> object, index to build the mesh
rho	vector of AR coefficients of length <code>p</code> (should satisfy stationarity conditions)
order	integer, the AR order <code>p</code> . If provided and <code>rho</code> is not specified, <code>rho</code> will be initialized as <code>rep(0, p)</code>

Value

ngme_operator object

Examples

```
# AR(2) model with specified coefficients
ar(c(1:10), rho = c(0.5, -0.3))
# AR(3) model with specified coefficients
ar(c(1:10), rho = c(0.4, 0.2, -0.1))
# AR(2) model with default coefficients (zeros)
ar(c(1:10), order = 2)
# AR(3) model with specified order and coefficients
ar(c(1:10), order = 3, rho = c(0.4, 0.2, -0.1))
```

ar1	<i>ngme AR(1) model specification</i>
-----	---------------------------------------

Description

ngme AR(1) model specification

Usage

```
ar1(mesh = NULL, rho = 0)
```

Arguments

mesh	integer vector or inla.mesh.1d object, index to build the mesh
rho	the correlation parameter (between -1 and 1)

Value

ngme_operator object

argo_float	<i>Argo float dataset</i>
------------	---------------------------

Description

Argo floats measurements.

Usage

```
data("argo_float")
```

Format

Data frame containing 274 observations on 4 variables.

lat Latitude.

lon Longitude.

sal Salinity.

temp Temperature.

Details

The floats have a pressure case made of aluminium that is about 1.3m long and about 20cm diameter. They weigh about 40kg. On the top is an antenna to communicate with the satellites that fix the float's position and receive the data. Also on the top are the temperature, salinity and pressure sensors.

Source

Data can be obtained from [Argo float website](#).

arma	<i>ngme ARMA(p, q) model specification</i>
------	--

Description

General ARMA(p, q) latent operator under AZW: $K W = Z \text{ eps}$, where K encodes the AR part and Z encodes the MA part.

Usage

```
arma(
  mesh = NULL,
  ar_order = 1,
  ma_order = 1,
  ar = NULL,
  ma = NULL,
  fix_ar = FALSE,
  fix_ma = FALSE
)
```

Arguments

mesh	Integer vector or 'inla.mesh.1d' object.
ar_order	Integer p (0, 1, or 2).
ma_order	Integer q (0, 1, or 2).
ar	Numeric length-p vector of AR coefficients in (-1, 1). Defaults to zeros.
ma	Numeric length-q vector of MA coefficients in (-1, 1). Defaults to zeros.
fix_ar	Logical or length-p logical vector to fix AR coefficients.
fix_ma	Logical or length-q logical vector to fix MA coefficients.

Details

- Supports $p, q \leq 2$. The user provides standard AR/MA coefficients (ar, ma). For estimation, these are transformed in R into an unbounded parameter vector θ_K via PACF-style mappings so optimizers (e.g., Adam/SGD) operate on unconstrained variables while K and Z remain valid: - AR(1): $\phi_1 = \tanh(\text{raw}_1/2)$. AR(2): $\pi_1 = \tanh(\text{raw}_1/2), \pi_2 = \tanh(\text{raw}_2/2), \phi_2 = \pi_2, \phi_1 = \pi_1 * (1 - \pi_2)$. - MA(1): $\theta_1 = \tanh(\text{raw}_1/2)$. MA(2): $\psi_1 = \tanh(\text{raw}_1/2), \psi_2 = \tanh(\text{raw}_2/2), \theta_2 = \psi_2, \theta_1 = \psi_1 * (1 - \psi_2)$. - The returned operator includes both K (AR part) and Z (MA part). During estimation the backend updates Z synchronously every time θ_K changes.

Value

An `ngme_operator` describing the ARMA(p, q) latent model.

Examples

```
mesh <- 1:10
op <- arma(mesh, ar_order = 2, ma_order = 2, ar = c(0.5, 0.3), ma = c(0.6, 0.4))
```

 arma11

Convenience wrapper for ARMA(1,1)

Description

Convenience wrapper for ARMA(1,1)

Usage

```
arma11(mesh = NULL, ar = 0, ma = 0, fix_ar = FALSE, fix_ma = FALSE)
```

Arguments

<code>mesh</code>	Integer vector or <code>'inla.mesh.1d'</code> object.
<code>ar</code>	Numeric length- p vector of AR coefficients in $(-1, 1)$. Defaults to zeros.
<code>ma</code>	Numeric length- q vector of MA coefficients in $(-1, 1)$. Defaults to zeros.
<code>fix_ar</code>	Logical or length- p logical vector to fix AR coefficients.
<code>fix_ma</code>	Logical or length- q logical vector to fix MA coefficients.

Value

An `ngme_operator` object describing an ARMA(1,1) latent operator. The object contains the AR precision component K , the MA filter component Z , integration weights h , and the unconstrained AR and MA parameters used by the optimizer. If `mesh` is `NULL`, returns an `ngme_operator_def` specification for delayed construction inside `f()`.

batch_decay *Batch/checkpoint decay helper*

Description

Batch/checkpoint decay helper

Usage

```
batch_decay(
  patience = 3,
  gamma = 0.5,
  min_delta = 0,
  warmup = 0,
  min_stepsize = 0
)
```

Arguments

patience	number of consecutive checkpoints without improvement before decay.
gamma	decay factor in $(0, 1)$.
min_delta	minimum required decrease to count as improvement.
warmup	number of initial checkpoints to skip.
min_stepsize	lower bound for absolute stepsize.

Details

Convenience helper that enables grad-norm plateau decay and keeps iteration schedule constant.

Value

a `stepsize_control()` object.

batch_means_ci *Pooled Batch-Means Confidence Intervals from Multiple Chains*

Description

Compute pooled point estimates, covariance, and Wald confidence intervals from multiple chain trajectories.

Usage

```
batch_means_ci(
  chain_trajectories,
  level = 0.95,
  alpha = 0.501,
  M = NULL,
  N = NULL,
  drop_burnin = TRUE,
  burnin_iter = 0
)
```

Arguments

chain_trajectories	list of numeric matrices, each with rows = iterations and columns = parameters.
level	confidence level.
alpha	stepsize decay exponent in $(1/2, 1)$.
M	number of retained batches per chain (excluding burn-in batch 0).
N	decorrelation constant used in the batch boundary formula.
drop_burnin	logical; if 'TRUE', discard batch 0.
burnin_iter	non-negative integer. Explicitly discard the first 'burnin_iter' iterations of each chain before Xi-style batching.

Value

A list with pooled estimates, covariance, standard errors, and confidence intervals.

batch_means_estimator *Batch-Means Covariance Estimator for SGD Trajectories*

Description

Estimate the asymptotic covariance from a single SGD trajectory using the increasing-batch construction from Xi et al. (2020).

Usage

```
batch_means_estimator(
  trajectory,
  alpha = 0.501,
  M = NULL,
  N = NULL,
  drop_burnin = TRUE,
  burnin_iter = 0
)
```

Arguments

trajectory	numeric matrix with rows = iterations and columns = parameters.
alpha	stepsize decay exponent in $\eta_i = \eta i^{-\alpha}$. Must satisfy $1/2 < \alpha < 1$.
M	number of retained batches (excluding burn-in batch 0). If 'NULL', use $\lfloor n^{(1-\alpha)/2} \rfloor$.
N	decorrelation constant in $e_k = \lfloor ((k+1)N)^{1/(1-\alpha)} \rfloor$. If 'NULL', use $N = n^{1-\alpha}/(M+1)$.
drop_burnin	logical; if 'TRUE', discard batch 0.
burnin_iter	non-negative integer. Explicitly discard the first 'burnin_iter' iterations before building Xi-style batches. After trimming, batch boundaries are rebuilt from iteration 1 of the retained trajectory.

Value

A list containing the covariance estimate, pooled mean, batch sizes, batch boundaries, and chain-level metadata.

bfgs

BFGS optimization

Description

BFGS optimization

Usage

```
bfgs(line_search = "wolfe")
```

Arguments

line_search	line search method, can be c("backtracking", "wolfe") "bfgs" means use BFGS preconditioner
-------------	--

Value

a list of control variables for optimization (used in `control_opt` function)

Description

Giving 2 sub_models, build a correlated bivariate operator based on $K = D(\theta, \rho)$

$$D(\theta, \rho) = \begin{pmatrix} \cos(\theta) + \rho \sin(\theta) & -\sin(\theta)\sqrt{1 + \rho^2} \\ \sin(\theta) - \rho \cos(\theta) & \cos(\theta)\sqrt{1 + \rho^2} \end{pmatrix}$$

Usage

```

bv(
  mesh,
  sub_models,
  theta = 0,
  rho = 0,
  c1 = 1,
  c2 = 1,
  share_param = FALSE,
  fix_theta = FALSE,
  use_c_param = FALSE
)

```

Arguments

mesh	the mesh where model is defined
sub_models	a list of sub_models (total 2 sub_models)
theta	the rotation parameter (starting point should be from -pi/4 to pi/4)
rho	the parameter related to correlation
c1	scaling factor for the first sub-model (default: 1)
c2	scaling factor for the second sub-model (default: 1)
share_param	TRUE if share the same parameter for 2 sub_models (of same type)
fix_theta	TRUE if fix the theta of bv model
use_c_param	TRUE to estimate c1 and c2 as parameters, FALSE to fix them at specified values (default: FALSE)

Details

The bivariate model combines two sub-models with a rotation matrix D and optional scaling factors $c1$ and $c2$. When `use_c_param = TRUE`, $c1$ and $c2$ are estimated as parameters (on log scale). When `use_c_param = FALSE` (default), $c1$ and $c2$ are fixed at their specified values (both default to 1).

Value

a `ngme_operator` of bivariate model

bv_matern

*Ngme bivariate model with Matern sub_models***Description**

Giving 2 sub_models, build a correlated bivariate operator based on $K = D(\theta, \rho)$

$$D(\theta, \rho) = \begin{pmatrix} \cos(\theta) + \rho \sin(\theta) & -\sin(\theta)\sqrt{1 + \rho^2} \\ \sin(\theta) - \rho \cos(\theta) & \cos(\theta)\sqrt{1 + \rho^2} \end{pmatrix}$$

Usage

```

bv_matern(
  mesh,
  sub_models,
  theta = 0,
  rho = 0,
  sd1 = 1,
  sd2 = 1,
  group = NULL,
  share_param = FALSE,
  fix_theta = FALSE,
  ...
)

```

Arguments

mesh	the mesh where model is defined
sub_models	a list of sub_models (should be two matern models)
theta	the parameter related to rotation
rho	the parameter related to correlation
sd1	scaling parameter for the first sub-model
sd2	scaling parameter for the second sub-model
group	group vector, can be inherited from ngme() function
share_param	TRUE if share the same parameter for 2 sub_models (of same type)
fix_theta	TRUE if the rotation parameter is fixed
...	ignore

Value

a list of specification of model

 calibrate_inv_exp_lambda_driven_nig

Calibrate Inverse-Exponential Prior for NIG Driven Noise

Description

Calibrate λ in the prior $\kappa = 1/\nu \sim \text{Exp}(\lambda)$ using a tail-inflation target for driven NIG noise.

The calibration target is

$$\Pr(R_c(\nu) > r_{\text{target}}) = \alpha,$$

where

$$R_c(\nu) = \frac{\Pr(|U| > c \mid \nu)}{\Pr(|Z| > c)}, \quad Z \sim N(0, 1)$$

and

$$U = \frac{\mu(V - h) + \sigma\sqrt{V}Z}{\sigma\sqrt{h}}, \quad V \sim \text{GIG}(-1/2, \nu, \nu h^2).$$

The function solves $R_c(\nu_r) = r_{\text{target}}$ using log-scale bisection, then returns

$$\lambda = -\nu_r \log(\alpha).$$

Usage

```
calibrate_inv_exp_lambda_driven_nig(
  r_target = 2,
  alpha = 0.1,
  c = 3,
  mu = 0,
  sigma = 1,
  h = 1,
  n_samples = 1e+05,
  nu_lower = 0.1,
  nu_upper = 100,
  tol = 0.05,
  max_iter = 30,
  max_expand = 30,
  seed = NULL
)

calibrate_inv_exp_lambda(...)
```

Arguments

<code>r_target</code>	target tail inflation level $r_{\text{target}} > 1$
<code>alpha</code>	target prior probability in $(0, 1)$
<code>c</code>	tail threshold for $ U > c$, typically ‘2.5’ or ‘3’

<code>mu</code>	NIG drift parameter in the driven noise term
<code>sigma</code>	NIG scale parameter (> 0)
<code>h</code>	positive increment scaling (> 0)
<code>n_samples</code>	Monte Carlo sample size used per evaluation of $R_c(\nu)$
<code>nu_lower</code>	initial lower bracket for ν
<code>nu_upper</code>	initial upper bracket for ν
<code>tol</code>	relative tolerance for solving $R_c(\nu_r) = r_{\text{target}}$
<code>max_iter</code>	maximum number of bisection iterations
<code>max_expand</code>	maximum bracket expansion steps on each side
<code>seed</code>	optional integer seed for reproducible calibration
<code>...</code>	arguments forwarded to <code>calibrate_inv_exp_lambda_driven_nig()</code>

Value

A list with calibrated ‘lambda’, solved ‘nu_r’, achieved ‘rc_nu_r’, and diagnostics.

cienaga

The swamp of Cienaga Grande in Santa Marta, Colombia

Description

There is a total of 114 locations where some properties of the swamp were measured. Those measurements were taken twice, however there is no information available about their chronological order so this data cannot be treated as spatiotemporal, despite that, the multiple measurements can be treated as replicates.

Usage

`cienaga`

Format

A data frame with 218 rows and 6 columns.

East, North location

depth depth of the swamp

temp temperature

oxyg oxygen

measurement 1 means the first measurement, 2 the second

Source

..

cienaga.border	<i>The x y location of the border of the swamp of Cienaga Grande in Santa Marta, Colombia</i>
----------------	---

Description

The data is of dimension 472 * 2. It contains the x and y coordinates of the border of the swamp.

Usage

```
cienaga.border
```

Format

A data frame with 472 rows and 2 columns.

East, North location

Source

..

compare_noise_kld	<i>Compare noise objects using Kullback-Leibler divergence</i>
-------------------	--

Description

This function compares multiple noise objects by calculating the KLD of each noise against the first noise object (reference).

Usage

```
compare_noise_kld(x = NULL, ..., xlim = c(-10, 10), n_points = 1000)
```

Arguments

x	first noise object (reference)
...	additional noise objects to compare, and optional parameters
xlim	x-axis range for evaluation (default: c(-10, 10))
n_points	number of evaluation points (default: 1000)

Value

named vector of KLD values

Examples

```
n1 <- noise_nig(mu = 0, sigma = 1, nu = 1)
n2 <- noise_nig(mu = 0.5, sigma = 1.2, nu = 0.8)
compare_noise_kld(n1, method2 = n2)
```

compute_index_corr_from_map

Helper function to compute the index_corr vector

Description

Helper function to compute the index_corr vector

Usage

```
compute_index_corr_from_map(map, eps = 0.1)
```

Arguments

map	used as location to compute distance, can be 1d (numerical) or 2d (data.frame)
eps	threshold to determine if two points are close (if close, we consider them as the same point)

Value

the index_corr vector for ngme correlated measurement noise

Examples

```
x_coord <- c(1.11, 1.12, 2, 1.3, 1.3)
y_coord <- c(2.11, 2.11, 2, 3.3, 3.3)
coord <- data.frame(x_coord, y_coord)
compute_index_corr_from_map(map = coord, 0.1)
```

compute_log_like

Compute Gaussian log-likelihood

Description

Creates the underlying C++ block models and evaluates their Gaussian log-likelihood when applicable.

Usage

```
compute_log_like(ngme_model)
```

Arguments

ngme_model An object created by 'ngme()'.

Value

A numeric scalar. Returns '0' if any replicate is non-Gaussian.

compute_ngme_ci	<i>Refit an Existing ngme Object with SGD and Compute Batch-Means CI</i>
-----------------	--

Description

Run one additional SGD stage (warm-started from an existing 'ngme' fit), then compute Xi-style batch-means confidence intervals from the newly stored trajectories.

Usage

```
compute_ngme_ci(
  fit,
  iterations = 4000,
  alpha = 0.501,
  optimizer = sgd(stepsize = 0.03),
  burnin = 100,
  n_batch = 20,
  n_parallel_chain = 4,
  t0 = 1,
  start_sd = 0.2,
  seed = Sys.time(),
  verbose = FALSE,
  level = 0.95,
  name = "all",
  M = NULL,
  N = NULL,
  apply_transform = TRUE,
  drop_burnin = TRUE,
  burnin_iter = 0,
  control_opt = NULL,
  ...
)
```

```
compute_ngme_CI(
  fit,
  iterations = 4000,
  alpha = 0.501,
  optimizer = sgd(stepsize = 0.03),
  burnin = 100,
```

```

n_batch = 20,
n_parallel_chain = 4,
t0 = 1,
start_sd = 0.2,
seed = Sys.time(),
verbose = FALSE,
level = 0.95,
name = "all",
M = NULL,
N = NULL,
apply_transform = TRUE,
drop_burnin = TRUE,
burnin_iter = 0,
control_opt = NULL,
...
)

```

Arguments

fit	existing fitted ‘ngme’ object (can be obtained with any optimizer).
iterations	optimization iterations for the SGD CI stage.
alpha	Xi-style exponent used for both polynomial schedule and batch-means inference.
optimizer	optimizer for the CI stage; must be ‘sgd(...)’ for Xi theory.
burnin	burn-in iterations before SGD optimization.
n_batch	number of optimization checkpoints.
n_parallel_chain	number of parallel chains for SGD.
t0	non-negative schedule offset in $\eta_t = \eta_0(t + t_0)^{-\alpha}$.
start_sd	standard deviation for randomized chain initialization.
seed	random seed for CI-stage optimization.
verbose	logical; print optimization progress.
level	confidence level for CI.
name	parameter block for CI (“all”, latent name, or “general”).
M	number of retained Xi batches (excluding batch 0).
N	decorrelation constant in Xi batch boundaries.
apply_transform	logical; if ‘TRUE’, apply Post-delta transform after raw-space inference.
drop_burnin	logical; if ‘TRUE’, discard Xi batch 0.
burnin_iter	non-negative integer used both as optimizer schedule warmup (‘stepsize_schedule_burnin_iter’) and as explicit CI trajectory trimming before Xi-style batching.
control_opt	optional pre-built ‘control_opt’ object for the CI stage. If supplied, it is used directly (with ‘store_traj’ forced to ‘TRUE’).
...	additional arguments forwarded to [control_opt_batch_ci()] when ‘control_opt’ is ‘NULL’.

Value

An object of class 'ngme_batch_ci' with extra fields: 'refit' (the SGD-refit model), 'refit_control_opt', and 'refit_source'.

compute_ngme_sgld_samples

Refit an Existing ngme Object with SGLD and Extract Samples

Description

Run one additional SGLD stage (warm-started from an existing 'ngme' fit), then extract posterior-like samples from stored trajectories.

Usage

```
compute_ngme_sgld_samples(
  fit,
  iterations = 4000,
  optimizer = sgld(stepsize = 0.01, temperature = 1),
  burnin = 100,
  n_batch = 20,
  n_parallel_chain = 4,
  alpha = 0.6,
  t0 = 10,
  start_sd = 0.2,
  seed = Sys.time(),
  verbose = FALSE,
  name = "all",
  burnin_iter = 0,
  thinning = 1,
  n_gibbs_samples = NULL,
  apply_transform = TRUE,
  combine_chains = TRUE,
  control_opt = NULL,
  ...
)
```

Arguments

fit	existing fitted 'ngme' object (can be obtained with any optimizer).
iterations	optimization iterations for the SGLD stage.
optimizer	optimizer for the sampling stage; must be 'sgld(...)'
burnin	burn-in iterations before optimization.
n_batch	number of optimization checkpoints.

n_parallel_chain	number of parallel chains.
alpha	polynomial schedule exponent used by 'poly_decay(alpha, t0)'.
t0	non-negative schedule offset.
start_sd	standard deviation for randomized chain initialization.
seed	random seed for SGLD stage.
verbose	logical; print optimization progress.
name	parameter block to extract: "all" (default), latent model name, or "general".
burnin_iter	non-negative integer used both as optimizer schedule warmup ('stepsize_schedule_burnin_iter') and as explicit trajectory trimming before sampling.
thinning	positive integer thinning interval.
n_gibbs_samples	optional positive integer. If supplied, override 'control_ngme\$n_gibbs_samples' for the SGLD refit stage only; otherwise inherit the value from 'fit'.
apply_transform	logical; apply parameter transforms to user scale.
combine_chains	logical; if 'TRUE', return one combined data.frame, otherwise return one data.frame per chain.
control_opt	optional pre-built 'control_opt' object for the SGLD stage. If supplied, it is used directly (with 'store_traj' forced to 'TRUE').
...	additional arguments forwarded to [control_opt()] when 'control_opt' is 'NULL'.

Value

A data.frame (or list of data.frames) from [ngme_sgl_d_samples()] with extra attributes 'refit', 'refit_control_opt', and 'refit_source'.

compute_score_given_pred

Compute the scores given the prediction

Description

Compute the scores given the prediction

Usage

```
compute_score_given_pred(
  Y_N_1_thin,
  Y_N_2_thin,
  y_data,
  group_data,
  merge_groups = FALSE,
  merged_group_name = NULL,
  metric = NULL
)
```

Arguments

Y_N_1_thin	posterior predictive draws (rows = observations, columns = samples)
Y_N_2_thin	posterior predictive draws (rows = observations, columns = samples)
y_data	a vector of length n_obs
group_data	a vector of length n_obs
merge_groups	logical, if TRUE and there are exactly two groups, combine them into a vector-valued score
merged_group_name	optional label for the merged group
metric	optional custom metric function used to combine group-wise values before scoring

control_ngme

Generate control specifications for the ngme model

Description

Generate control specifications for the ngme model

Usage

```
control_ngme(
  n_gibbs_samples = 5,
  fix_beta = FALSE,
  n_post_samples = 100,
  beta_init = NULL,
  debug = FALSE,
  ...
)
```

Arguments

n_gibbs_samples	number of gibbs samples at each iteration
fix_beta	logical, fix fixed effect estimation
n_post_samples	number of posterior samples, see ?ngme_post_samples()
beta_init	fixed effect initial value on the original design scale. If control_opt(standardize_fixed = TRUE) (the default), the vector is internally rotated/scaled to match the SVD-standardized design matrix before being passed to the optimizer. Provide values on the raw design scale; no manual rescaling is required.
debug	debug mode
...	additional arguments. Legacy aliases feff and fix_feff are still recognized and mapped to beta_init and fix_beta.

Value

a list of control variables for ngme

control_opt	<i>Generate control specifications for ngme() function.</i>
-------------	---

Description

These are configurations for ngme optimization process.

Usage

```
control_opt(
  seed = Sys.time(),
  burnin = 100,
  iterations = 500,
  estimation = TRUE,
  standardize_fixed = TRUE,
  n_batch = 10,
  iters_per_check = iterations/n_batch,
  optimizer = adam(),
  start = NULL,
  start_sd = 0.5,
  n_parallel_chain = 4,
  max_num_threads = n_parallel_chain,
  print_check_info = FALSE,
  max_relative_step = 0.5,
  max_absolute_step = 0.5,
  rao_blackwellization = FALSE,
  n_trace_iter = 10,
  sampling_strategy = "all",
  solver_backend = "cholmod",
  solver_type = "llt",
  verbose = FALSE,
  store_traj = TRUE,
  robust = FALSE,
  stepsize_control = NULL,
  n_min_batch = min(n_batch, 3),
  n_slope_check = min(n_batch, 3),
  trend_std_conv_check = TRUE,
  std_lim = 0.01,
  trend_lim = 0.01,
  R_hat_conv_check = TRUE,
  max_R_hat = 1.1,
  pflug_conv_check = TRUE,
  pflug_alpha = 0.9
)
```

Arguments

seed	set the seed for pseudo random number generator
burnin	iterations for burn-in periods (before optimization)
iterations	optimization iterations
estimation	run the estimation process (call C++ in backend)
standardize_fixed	whether or not standardize the fixed effect. When TRUE (default), the design matrix is SVD-standardized internally and any user-supplied control_ngme(beta_init = ...) is automatically mapped from the original design scale to that standardized basis. Set to FALSE to keep both the design matrix and any provided beta_init on their original scale.
n_batch	number of checkpoints; optimization is split into n_batch equal batches
iters_per_check	run how many iterations between each check point (or specify n_batch)
optimizer	choose different sgd optimization method, currently support "sgd", "sgld", "precond_sgd", "momentum", "adagrad", "rmsprop", "adam", "adamW" see ?sgd, ?precond_sgd, ?momentum, ?adagrad, ?rmsprop, ?adam, ?adamW
start	deprecated guard argument. Do not pass model starts through control_opt(); use ngme(..., start = previous_fit) instead.
start_sd	standard deviation of the initial parameter (1st chain fixed, other chains random), set 0 to be fixed for all chains
n_parallel_chain	number of parallel chains
max_num_threads	maximum number of threads used for parallel computing, by default will be set same as n_parallel_chain. If it is more than n_parallel_chain, the rest will be used to parallel different replicates of the model.
print_check_info	print the convergence information
max_relative_step	max relative step allowed in 1 iteration
max_absolute_step	max absolute step allowed in 1 iteration
rao_blackwellization	use rao_blackwellization
n_trace_iter	use how many iterations to approximate the trace (Hutchinson's trick)
sampling_strategy	subsampling method of replicates of model, c("all", "ws") "all" means using all replicates in each iteration, "ws" means weighted sampling (each iteration use 1 replicate to compute the gradient, the sample probability is proportion to its number of observations)
solver_backend	backend in ("eigen", "cholmod", "pardiso")
solver_type	factorization type: "llt" or "ldlt"

verbose	print estimation
store_traj	store the optimizer trajectory for diagnostics (set FALSE to reduce memory)
robust	use robust mode in the backend optimizer/model updates
stepsize_control	unified stepsize configuration created by stepsize_control(), poly_decay(), or batch_decay(). For polynomial schedule, poly_decay(..., burnin_iter = B) keeps schedule scale at 1 for the first B iterations, then starts decay with reset local time index.
n_min_batch	minimum number of checkpoints before any convergence diagnostic is attempted
n_slope_check	number of checkpoints used as the regression window for the trend test
trend_std_conv_check	enable the trend/std diagnostic (uses std_lim, trend_lim, n_slope_check)
std_lim	maximum allowed standard deviation
trend_lim	maximum allowed slope
R_hat_conv_check	use the R-hat diagnostic for convergence checking
max_R_hat	maximum allowed R_hat
pflug_conv_check	use Pflug diagnostic for convergence check
pflug_alpha	scaling factor (0-1] for Pflug criterion: require pflug_sum < pflug_alpha * max_pflug_sum

Details

Convergence diagnostics (multi-chain): * R-hat: per-parameter Gelman–Rubin statistic; passes if $R_{\text{hat}} \leq \max_{\text{R_hat}}$. * Trend/Std: uses the last `n_slope_check` checkpoints after at least `n_min_batch` batches. Passes when both the relative std ($\sqrt{\text{var}}/|\text{mean}| \leq \text{std_lim}$) and linear trend of the means ($|\text{slope}| \leq \text{trend_lim}$) satisfy their thresholds. * Pflug: per-chain criterion $\text{pflug_sum} < \text{pflug_alpha} * \max_{\text{pflug_sum}}$ in the latest batch; if all chains satisfy it, overall convergence is declared. Checks are evaluated every `iters_per_check = iterations / n_batch`. A parameter is marked converged if any enabled parameter-level diagnostic (R-hat or Trend/Std) passes; the run stops when all parameters converge or when the Pflug diagnostic triggers.

Value

list of control variables

control_opt_batch_ci *Generate CI-focused control settings for batch-means inference*

Description

Convenience wrapper for control_opt() with defaults tailored for Xi-style batch-means confidence intervals.

Usage

```
control_opt_batch_ci(
  optimizer = sgd(stepsize = 0.03),
  burnin = 100,
  iterations = 2000,
  n_batch = 20,
  n_parallel_chain = 4,
  alpha = 0.501,
  t0 = 1,
  schedule_burnin_iter = 0,
  ...
)
```

Arguments

optimizer	optimizer object, default <code>sgd(stepsize = 0.03)</code> .
burnin	burn-in iterations before optimization.
iterations	optimization iterations.
n_batch	number of checkpoints.
n_parallel_chain	number of parallel chains.
alpha	polynomial stepsize exponent for <code>poly_decay(alpha, t0)</code> .
t0	non-negative schedule offset.
schedule_burnin_iter	non-negative integer. Initial optimization iterations where polynomial schedule scaling is disabled.
...	additional arguments forwarded to <code>control_opt()</code> to override defaults.

Details

This helper enforces trajectory-friendly defaults:

- `store_traj = TRUE`
- `trend_std_conv_check = FALSE`
- `R_hat_conv_check = FALSE`
- `pflug_conv_check = FALSE`
- `stepsize_control = poly_decay(alpha, t0, schedule_burnin_iter)`

Any of these can still be overridden through

Value

object of class `control_opt`.

`create_paired_cv_splits`

Create paired indices for bivariate cross-validation Ensures that paired observations (e.g., u_wind and v_wind at same location) are kept together in the same fold

Description

Create paired indices for bivariate cross-validation Ensures that paired observations (e.g., u_wind and v_wind at same location) are kept together in the same fold

Usage

```
create_paired_cv_splits(data, loc_col, group, k, seed = NULL)
```

Arguments

data	data frame containing the observations
loc_col	character vector of column names defining locations (e.g., c("lon", "lat") or c("x", "y"))
group	character, name of the group column (e.g., "direction" for wind data)
k	number of folds
seed	random seed

Value

list with test_idx and train_idx, each containing k lists of indices

Examples

```
# Example with wind data
data_long <- data.frame(
  lon = rep(c(1, 2, 3, 4), 2),
  lat = rep(c(1, 1, 2, 2), 2),
  direction = rep(c("u_wind", "v_wind"), each = 4),
  wind = rnorm(8)
)
splits <- create_paired_cv_splits(data_long, c("lon", "lat"), "direction", k = 2)
```

cross_validation	<i>Compute the cross-validation for the ngme model Perform cross-validation for ngme model first into sub_groups (a list of target, and train data)</i>
------------------	---

Description

Compute the cross-validation for the ngme model Perform cross-validation for ngme model first into sub_groups (a list of target, and train data)

Usage

```
cross_validation(
  ngme,
  type = "k-fold",
  seed = NULL,
  print = TRUE,
  N_sim = 5,
  n_gibbs_samples = 500,
  n_burnin = 100,
  k = 5,
  percent = 0.2,
  times = 10,
  metric = NULL,
  test_idx = NULL,
  train_idx = NULL,
  keep_pred = FALSE,
  parallel = FALSE,
  thinning_gap = 1,
  cores_layer1 = if (parallel) min(parallel::detectCores(), 2) else 1,
  cores_layer2 = if (parallel) min(parallel::detectCores(), 2) else 1,
  merge_groups = FALSE,
  merged_group_name = NULL,
  data = NULL,
  chain_combine = c("param_mean", "predictive_average")
)
```

Arguments

ngme	a ngme object, or a list of ngme object (if comparing multiple models)
type	character, in c("k-fold", "loo", "lpo", "custom") k-fold is k-fold cross-validation, provide k loo is leave-one-out, lpo is leave-percent-out, provide percent from 1 to 100 custom is user-defined group, provide target and data
seed	random seed
print	print information during computation
N_sim	integer, number of simulations (e.g., estimate MAE, MSE, .. N times)

n_gibbs_samples	number of gibbs samples of latent process, used for computing CRPS, sCRPS
n_burnin	number of burnin
k	integer (only for k-fold type)
percent	how many percent for testing? from 0 to 1 (for lpo type)
times	how many test cases (only for lpo type)
metric	Optional function or list of functions (one per model) that maps the group-wise observations/predictions for a single location to the quantity that should be scored. The function receives a list containing at least y (a named numeric vector of group values) and may optionally use samples1 and samples2 (matrices with rows named by group and columns indexing posterior draws). The function must return either a numeric scalar (optionally named), or a list with component y and optional components samples1, samples2, and label. When NULL, the original per-group scores are computed. Example: <code>metric = function(data) 2 * data\$y["A"] + data\$y["B"]</code> . To sum all groups, return <code>sum(data\$y)</code> .
test_idx	a list of indices of the data (which data points to be predicted) (only for custom type)
train_idx	a list of indices of the data (which data points to be used for re-sampling (not re-estimation)) (only for custom type)
keep_pred	logical, keep test information (pred_1, pred_2) in the return (as attributes), pred_1 and pred_2 are the prediction of the two chains
parallel	logical, run in parallel mode
thining_gap	integer, the gap between samples for thinning, if 0, then no thinning, if 1, then keep 50% of the samples for CRPS, sCRPS, etc.
cores_layer1	integer, number of cores for the first layer (over testing samples)
cores_layer2	integer, number of cores for the second layer (over computing scores for N_sim simulations)
merge_groups	logical, if TRUE, merge groups as vector components (e.g., for vector-valued wind data with north_wind, east_wind). MAE becomes Euclidean distance, MSE becomes squared Euclidean distance, etc.
merged_group_name	character, name for the merged group when merge_groups=TRUE. If NULL, uses "group1_group2" format (default: NULL)
data	optional data.frame used to replace the original fitting data before running CV. If 'NULL', the data stored in 'ngme' is used. If provided, the model is rebuilt on 'data' while reusing fitted parameters from 'ngme'.
chain_combine	how to combine multiple optimization chains: "param_mean" uses the fitted object directly (default), while "predictive_average" computes predictions from each optimization chain and averages at the predictive level.

Value

A list with components:

mean.scores Mean of the N_sim estimates for MSE, MAE, CRPS, and sCRPS.

sd.scores Standard deviation of the N_sim estimates for MSE, MAE, CRPS, and sCRPS.

Description

Function used for defining of smooth and spatial terms within ngme model formulae. The function is a wrapper function for specific submodels. (see `ngme_models_types()` for available models).

Usage

```
f(
  map,
  model,
  noise = noise_normal(),
  name = "field",
  data = NULL,
  group = NULL,
  which_group = NULL,
  replicate = NULL,
  A = NULL,
  W = NULL,
  fix_W = FALSE,
  fix_K = FALSE,
  prior = NULL,
  subset = rep(TRUE, length_map(map)),
  debug = FALSE
)
```

Arguments

<code>map</code>	symbol or numerical value: index or covariates to build index
<code>model</code>	an <code>ngme_operator</code> or <code>ngme_operator_def</code> created by model constructors such as <code>ar1()</code> , <code>matern()</code> , <code>bv()</code> , etc.
<code>noise</code>	<code>ngme_noise</code> object, <code>noise_nig()</code> or <code>noise_gal()</code>
<code>name</code>	name of the field, for later use, if not provided, will be "field1" etc.
<code>data</code>	specified or inherit from <code>ngme()</code> function
<code>group</code>	group factor indicate resposne variable, can be inherited from <code>ngme()</code> function, (used for bivariate model)
<code>which_group</code>	belong to which group
<code>replicate</code>	factor indicating replicate structure for INLA-style replicates. When provided, operators and A matrices will be block-diagonalized across replicates.
<code>A</code>	observation matrix, automatically computed given <code>map</code> and <code>model</code>
<code>W</code>	starting value of the process
<code>fix_W</code>	stop sampling for W

<code>fix_K</code>	fix the estimation of parameter of K
<code>prior</code>	prior specification created by <code>prior_*</code> () or <code>priors(...)</code> for operator parameters (<code>theta_K</code>).
<code>subset</code>	subset of the model
<code>debug</code>	debug mode

Details

When using different meshes for different replicates, provide the mesh parameter as a list of mesh objects. The number of meshes should match the number of replicates. For example: `mesh = list(mesh1, mesh2, mesh3)` for 3 replicates.

When using the ‘replicate’ argument, the operator matrices will be block-diagonalized. For a generic operator $K = \text{param1} * \text{Matrix1} + \text{param2} * \text{Matrix2}$, with 2 replicates, the resulting operator becomes: $K = \text{param1} * \text{bdiag}(\text{Matrix1_rep1}, \text{Matrix1_rep2}) + \text{param2} * \text{bdiag}(\text{Matrix2_rep1}, \text{Matrix2_rep2})$ Similarly, the A matrix will be block-diagonalized as `bdiag(A_rep1, A_rep2, ...)`.

Value

a list for constructing latent model, e.g. A, h, C, G, which also has 1. Information about K matrix
2. Information about noise
3. Control variables

gal

The Generalized Asymmetric Laplace (GAL) Distribution

Description

Density, distribution function, quantile function and random generation for the generalized asymmetric Laplace distribution with parameters `mu`, `sigma` and `nu`, `delta`.

Usage

```
dgal(x, delta, mu, nu, sigma, log = FALSE)
```

```
rgal(n, delta, mu, nu, sigma, seed = 0)
```

```
pgal(q, delta, mu, nu, sigma, lower.tail = TRUE, log.p = FALSE)
```

```
qgal(p, delta, mu, nu, sigma, lower.tail = TRUE, log.p = FALSE)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>delta</code>	A numeric value for the location parameter.
<code>mu</code>	A numeric value for the shift parameter.
<code>nu</code>	A numeric value for the shape parameter.

sigma	A numeric value for the scaling parameter.
log, log.p	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
n	number of observations.
seed	Seed for the random generation.
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
p	vector of probabilities.

Details

The generalized asymmetric Laplace distribution has density given by

$$f(x; p, a, b) = \frac{e^{\nu + \mu(x - \delta)/\sigma^2} \sqrt{\nu\mu^2/\sigma^2 + \nu^2}}{\pi \sqrt{\nu\sigma^2 + (x - \delta)^2}} K_1(\sqrt{(\nu\sigma^2 + (x - \delta)^2)(\mu^2/\sigma^4 + \nu/\sigma^2)}),$$

where K_p is modified Bessel function of the second kind of order p , $x > 0$, $\nu > 0$ and $\mu, \delta, \sigma \in \mathbb{R}$. See Barndorff-Nielsen (1977, 1978 and 1997) for further details.

If the mixing variable V follows a Gamma distribution (same parameterization in R):

$$V \sim \Gamma(h\nu, \nu),$$

then the posterior follows the GAL distribution (a special case of GIG distribution):

$$-\mu + \mu V + \sigma\sqrt{V}Z \sim GIG(h\nu - 0.5, 2\nu + (\frac{\mu}{\sigma})^2, 0)$$

Value

dgal gives the density, pgal gives the distribution function, qgal gives the quantile function, and rgal generates random deviates.

Invalid arguments will result in return value NaN, with a warning.

The length of the result is determined by n for rgal.

References

Barndorff-Nielsen, O. (1977) Exponentially decreasing distributions for the logarithm of particle size. Proceedings of the Royal Society of London.

Series A, Mathematical and Physical Sciences. The Royal Society. 353, 401–409. doi:10.1098/rspa.1977.0041

Barndorff-Nielsen, O. (1978) Hyperbolic Distributions and Distributions on Hyperbolae, Scandinavian Journal of Statistics. 5, 151–157.

See Also

[dgig](#), [dig](#), [digam](#)

Examples

```

rgal(100, delta = 0, mu = 5, sigma = 1, nu = 1)
pgal(0.4, delta = 0, mu = 5, sigma = 1, nu = 1)
qgal(0.8, delta = 0, mu = 5, sigma = 1, nu = 1)
plot(function(x){dgal(x, delta = 0, mu = 5, sigma = 1, nu = 1)}, main =
"generalized asymmetric Laplace density", ylab = "Probability density",
xlim = c(0,10))

```

generic

Generic precision matrix operator

Description

Creates a flexible precision matrix K by allowing linear combinations of base matrices with parameter-dependent coefficients. The model follows the form: $K = \sum_i f_i(\theta) * matrices_i$, where f_i depends on the parameter transformation.

Usage

```

generic(
  theta_K,
  matrices,
  h,
  trans = NULL,
  mesh = NULL,
  zero_trace = FALSE,
  model = "generic",
  param_name = NULL,
  param_trans = NULL,
  ...
)

```

Arguments

theta_K	The parameter vector (in real scale). If missing, initialized as double(0)
matrices	A list of matrices to be combined with parameter-dependent coefficients
h	The integration weights vector
trans	Transformation for each parameter. Must be a list where each element is a character vector defining transformations for each matrix. For example, 'trans=list(kappa=c("exp2", "identity", "null"))' means parameter 'kappa' affects matrix 1 with exp2 transformation, matrix 2 with identity, and doesn't affect matrix 3. Available transformations: "identity", "exp", "exp2", "exp4", "sqrt", "square", "log", "tanh"
mesh	The mesh object
zero_trace	Whether the trace of K should be zero
model	The model type name

param_name	Optional parameter names stored on the returned operator for diagnostics
param_trans	Optional parameter transformations stored on the returned operator for diagnostics
...	Additional arguments (ignored)

Details

This function can be used to represent various models like AR1, Matern, and RW1 in a unified framework.

The ‘generic’ function provides a flexible way to construct precision matrices by combining existing matrices with transformed parameters. Here’s how it works:

1. Each parameter in ‘theta_K’ can affect one or more matrices in the ‘matrices’ list
2. The ‘trans’ list defines how each parameter transforms before multiplying each matrix
3. For each matrix, the coefficients from all parameters are multiplied together
4. The final K is the sum of all transformed matrices

Common use cases:

- **AR1 model**: $K = \rho * C + G$ (where ρ is between -1 and 1) - **Matern (alpha=2)**: $K = \kappa^2 * C + G$ (where $\kappa > 0$) - **Matern (alpha=4)**: $K = \kappa^4 * C + 2 * \kappa^2 * G + G * C_{inv} * G$

Value

An object of class `ngme_operator`. The object stores the sparse precision matrix K, integration weights h, parameter vector theta_K, base matrices, transformation specification trans, and an update_K function that rebuilds K for new parameter values. It is intended for use as the latent model inside `f()`.

Examples

```
# AR1 model with rho = 0.5
ar1_obj <- ar1(1:10, rho = 0.5)
g <- name2fun("tanh", inv = TRUE)
generic_ar1 <- generic(
  theta_K = c(rho = g(0.5)), # Transform from real scale
  trans = list(rho = c("tanh", "null")), # Apply tanh to first matrix
  matrices = list(ar1_obj$C, ar1_obj$G),
  h = ar1_obj$h
)

# Matern model with kappa = 2
mesh <- fmesher::fm_mesh_1d(seq(0, 1, length.out = 10))
matern_obj <- matern(mesh)
log_kappa <- log(2)
generic_matern <- generic(
  theta_K = c(kappa = log_kappa),
  trans = list(kappa = c("exp2", "null")), # exp(2*kappa) for C, nothing for G
  matrices = list(matern_obj$C, matern_obj$G),
  h = matern_obj$h
)
```

```

# Matern model with alpha = 4 and kappa = 2
set.seed(1)
mesh <- fmesher::fm_mesh_2d(cbind(x = runif(20), y = runif(20)))
matern_obj <- matern(mesh, alpha = 4)
C <- matern_obj$C
G <- matern_obj$G
Cinv <- C; diag(Cinv) <- 1 / Matrix::diag(C)

generic_matern4 <- generic(
  theta_K = c(kappa = log(2)),
  trans = list(kappa = c("exp4", "exp2", "null")),
  matrices = list(C, 2*G, G %**% Cinv %**% G),
  h = matern_obj$h
)

```

generic_ns	<i>Non-stationary precision matrix operator with custom matrix combinations</i>
------------	---

Description

Creates a flexible non-stationary precision matrix K by allowing both linear combinations and matrix multiplications with parameter-dependent diagonal matrices. This enables modeling spatially varying parameters through basis expansions.

Usage

```

generic_ns(
  theta_K,
  matrices,
  position,
  h,
  model = "generic_ns",
  B_theta_K = NULL,
  trans = NULL,
  mesh = NULL,
  zero_trace = FALSE,
  param_name = NULL,
  param_trans = NULL,
  ...
)

```

Arguments

theta_K	List of parameter vectors (in real scale)
matrices	List of fixed matrices to be used in the model

position	List of vectors specifying matrix combinations (required)
h	The integration weights vector
model	The model type name stored on the returned operator
B_theta_K	List of basis matrices for parameters, defaults to matrices of 1s if not provided
trans	List of transformations for each parameter (one transformation per parameter)
mesh	The mesh object
zero_trace	Whether the trace of K should be zero
param_name	Optional parameter names stored on the returned operator for diagnostics
param_trans	Optional parameter transformations stored on the returned operator for diagnostics
...	Additional arguments (ignored)

Details

The key distinction from 'generic' is that 'generic_ns': 1. Requires explicit position specification for matrix combinations 2. Converts parameters to diagonal matrices for multiplication with fixed matrices 3. Allows for basis expansions via B_theta_K

The 'generic_ns' operator constructs K through the following steps:

1. Create diagonal matrices for each parameter using basis expansions: $D_{\text{param}} = \text{diag}(B_{\text{param}} * \text{theta}_{\text{param}})$
2. Combine parameter matrices with fixed matrices according to position specifications
3. Sum all the resulting combinations

The 'position' parameter defines how matrices are combined: - Each element of the list represents a term in the sum - Each vector contains indices of matrices to multiply (parameter matrices first, then fixed matrices) - For example: 'position = list(c(1, 3), c(2, 4))' with one parameter means: Multiply the parameter diagonal matrix (index 1) with fixed matrix 1 (index 3), then add parameter diagonal matrix 2 (index 2) multiplied by fixed matrix 2 (index 4)

Spatially-varying parameters can be created using basis matrices in B_theta_K.

Value

An object of class `ngme_operator`. The object stores the sparse non-stationary precision matrix K, integration weights h, the flattened parameter vector `theta_K`, basis matrices `B_theta_K`, parameter grouping metadata `param_map`, matrix combination rules `position`, and an update function for rebuilding K. It is intended for use as the latent model inside `f()`.

Examples

```
# Simple example with one parameter
n <- 5
A <- matrix(1, n, n)
B <- matrix(2, n, n)
alpha <- 0.4

# Create a simple generic_ns model: D_alpha * A + B
model <- generic_ns(
  theta_K = list(alpha = c(alpha)),
```

```

    matrices = list(A, B),
    position = list(c(1, 2), c(3)), # D_alpha * A + B
    h = rep(1, n)
  )

  # AR1 model representation: rho * C + G
  ar1_obj <- ar1(1:10, rho = 0.5)
  g <- name2fun("tanh", inv = TRUE)
  generic_ar1 <- generic_ns(
    theta_K = list(x = c(g(0.5))), # Transform from real scale
    trans = list(x = "tanh"), # Apply tanh transformation
    matrices = list(ar1_obj$C, ar1_obj$G),
    position = list(c(1, 2), c(3)), # D_rho * C + G
    h = ar1_obj$h,
    mesh = 1:10
  )

  # Spatially varying Matern model
  # Create a simple 1D mesh
  mesh <- fmesher::fm_mesh_1d(seq(0, 1, length.out = 10))

  # Create basis for spatially-varying kappa
  n <- 10
  B_kappa <- matrix(0, n, 2)
  B_kappa[1:(n / 2), 1] <- 1 # First half of the domain
  B_kappa[(n / 2 + 1):n, 2] <- 1 # Second half of the domain

  # Create standard Matern components
  matern_model <- matern(mesh)

  # Create model with space-varying kappa
  ns_model <- generic_ns(
    theta_K = list(kappa = c(log(1), log(2))), # Different values for each region
    matrices = list(matern_model$C, matern_model$G),
    B_theta_K = list(kappa = B_kappa),
    trans = list(kappa = "exp2"), # kappa^2 transformation for C
    h = matern_model$h,
    position = list(c(1, 2), c(3)), # D_kappa * C + G
    mesh = mesh
  )

```

get_data_from_formula *Extracts design matrix from a formula and data.*

Description

This function takes a formula and a data frame, and returns a design matrix based on the right-hand side of the formula. If the formula is '~.', it treats all columns in the data as the design matrix. Otherwise, it constructs a design matrix without an intercept based on the specified formula.

Usage

```
get_data_from_formula(form, data)
```

Arguments

form A formula object, e.g., '~ x1 + x2' or '~.'.
 data A data frame or matrix from which to extract the design matrix.

Value

A numeric matrix representing the design matrix.

Examples

```
data(mtcars)
# Extract a design matrix for 'mpg' and 'cyl'
X1 <- get_data_from_formula(~ mpg + cyl, mtcars)
# Extract a design matrix for all columns
X2 <- get_data_from_formula(~., mtcars)
# Extract a design matrix for 'hp'
X3 <- get_data_from_formula(~hp, mtcars)
```

```
get_parameter_distance
```

Calculate parameter distance from true values

Description

Compute $\| \theta - \hat{\theta} \|$ distance for all parameters across iterations. This provides a single measure of convergence combining all parameters.

Usage

```
get_parameter_distance(
  trajectories,
  true_values,
  norm_type = "euclidean",
  chain_summary = "mean"
)
```

Arguments

trajectories ngme_trajectories object from get_trace_trajectories()
 true_values named list or vector of true parameter values
 norm_type character, type of norm to use: "euclidean" (default), "manhattan", "max"
 chain_summary character, how to summarize across chains: "mean" (default), "median", "chain1"

Value

numeric vector of distances across iterations

get_trace_trajectories

Get trace trajectories from ngme fitting

Description

Extract numerical trajectories of parameters during ngme optimization without creating plots. This function provides the underlying data used by traceplot().

Usage

```
get_trace_trajectories(ngme, name = "general", apply_transform = TRUE)
```

Arguments

ngme	ngme object
name	name of latent models, otherwise get fixed effects and measurement noise should be in names(ngme\$models) or other
apply_transform	logical, whether to apply parameter transformations (default: TRUE)

Value

list containing:

trajectories named list of trajectory matrices for each parameter

parameter_names character vector of parameter names

transformations list of transformation functions used

n_chains number of chains

n_iterations number of iterations

get_trajectories	<i>get the trajectories of parameters of the model</i>
------------------	--

Description

Get the trajectories of the parameters of the model

Usage

```
get_trajectories(ngme_object, model_name)
```

Arguments

ngme_object	ngme object
model_name	name of the model, if NULL, return the trajectories of the parameters of the measurement noise and fixed effects

Value

a list of trajectories, each element is a matrix of trajectories ($n_samples * n_trajectories$)

gig	<i>The Generalised Inverse-Gaussian (GIG) Distribution</i>
-----	--

Description

Density, distribution function, quantile function and random generation for the generalised inverse-Gaussian distribution with parameters p , a and b .

Usage

```
dgig(x, p, a, b, log = FALSE)
rgig(n, p, a, b, seed = 0)
pgig(q, p, a, b, lower.tail = TRUE, log.p = FALSE)
qgig(prob, p, a, b, lower.tail = TRUE, log.p = FALSE)
```

Arguments

x, q	vector of quantiles.
p	parameter p.
a, b	parameters a and b. Must be positive.
log, log.p	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
n	number of observations.
seed	Seed for the random generation.
lower.tail	logical; if TRUE, probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
prob	vector of probabilities.

Details

The generalised inverse-Gaussian distribution has density given by

$$f(x; p, a, b) = ((a/b)^{p/2}) / (2K_p(\sqrt{ab})) x^{p-1} \exp\{-(a/2)x - (b/2)/x\},$$

where K_p is modified Bessel function of the second kind of order p , $x > 0$, $a, b > 0$ and $p \in \mathbb{R}$. See Jørgensen (1982) for further details.

Value

dgig gives the density, pgig gives the distribution function, qgig gives the quantile function, and rgig generates random deviates.

Invalid arguments will result in return value NaN, with a warning.

The length of the result is determined by n for rgig.

References

Jørgensen, Bent (1982). Statistical Properties of the Generalized Inverse Gaussian Distribution. Lecture Notes in Statistics. 9. New York–Berlin: Springer-Verlag. doi:10.1007/9781461256984

See Also

[dnig](#), [dig](#), [digam](#)

Examples

```
rgig(20, p = 1, a = 1, b = 1)
pgig(0.4, p = 1, a = 1, b = 1)
qgig(0.8, p = 1, a = 1, b = 1)
plot(function(x){dgig(x, p = 1, a = 1, b = 1)}, main =
"Generalised inverse-Gaussian density", ylab = "Probability density",
xlim = c(0,10))
```

 ig *The Inverse-Gaussian (IG) Distribution*

Description

Density, distribution function, quantile function and random generation for the inverse-Gaussian distribution with parameters a and b .

Usage

```
dig(x, a, b, log = FALSE)
```

```
rig(n, a, b, seed = 0)
```

```
pig(q, a, b, lower.tail = TRUE, log.p = FALSE)
```

```
qig(p, a, b, lower.tail = TRUE, log.p = FALSE)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>a, b</code>	parameters a and b . Must be positive.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>n</code>	number of observations.
<code>seed</code>	Seed for the random generation.
<code>lower.tail</code>	logical; if TRUE, probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>p</code>	vector of probabilities.

Details

The inverse-Gaussian distribution has density given by

$$f(x; a, b) = \frac{\sqrt{b}}{\sqrt{2\pi x^3}} \exp\left(-\frac{a}{2}x - \frac{b}{2x} + \sqrt{ab}\right),$$

where $x > 0$ and $a, b > 0$. In this parameterization, $E(X) = \sqrt{b}/\sqrt{a}$. See Tweedie (1957a, 1957b) for further details.

Value

`dig` gives the density, `pig` gives the distribution function, `qig` gives the quantile function, and `rig` generates random deviates.

Invalid arguments will result in return value NaN, with a warning.

The length of the result is determined by `n` for `rig`.

References

Tweedie, M. C. K. (1957a). "Statistical Properties of Inverse Gaussian Distributions I". *Annals of Mathematical Statistics*. 28 (2): 362–377. doi:10.1214/aoms/1177706964

Tweedie, M. C. K. (1957b). "Statistical Properties of Inverse Gaussian Distributions II". *Annals of Mathematical Statistics*. 28 (3): 696–705. doi:10.1214/aoms/1177706881

See Also

[dnig](#), [dgif](#), [digam](#)

Examples

```
rig(100, a = 1, b = 1)
pig(0.4, a = 1, b = 1)
qig(0.8, a = 1, b = 1)
plot(function(x){dig(x, a = 1, b = 1)}, main =
      "Inverse-Gaussian density", ylab = "Probability density",
      xlim = c(0,10))
```

 igam

The Inverse-Gamma (IGam) Distribution

Description

Density, distribution function, quantile function and random generation for the inverse-Gamma distribution with parameters a and b .

Usage

```
digam(x, a, b, log = FALSE)
```

```
rigam(n, a, b)
```

```
pigam(q, a, b, lower.tail = TRUE, log.p = FALSE)
```

```
qigam(p, a, b, lower.tail = TRUE, log.p = FALSE)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>a, b</code>	parameters a and b . Must be positive.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>n</code>	number of observations.
<code>lower.tail</code>	logical; if TRUE, probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>p</code>	vector of probabilities.

Details

The inverse-Gamma distribution has density given by

$$f(x; a, b) = \frac{b^a}{\Gamma(a)} x^{-a-1} \exp\left(-\frac{b}{x}\right),$$

where $x > 0$ and $a, b > 0$.

Value

digam gives the density, pigam gives the distribution function, qigam gives the quantile function, and rigam generates random deviates.

Invalid arguments will result in return value NaN, with a warning.

The length of the result is determined by n for rig.

See Also

[dnig](#), [dgig](#)

Examples

```
rigam(100, a = 1, b = 1)
pigam(0.4, a = 1, b = 1)
qigam(0.8, a = 1, b = 1)
plot(function(x){digam(x, a = 1, b = 1)}, main =
      "Inverse-Gamma density", ylab = "Probability density",
      xlim = c(0,10))
```

 iid

ngme iid model specification

Description

ngme iid model specification

Usage

```
iid(mesh = NULL)
```

Arguments

mesh integer or factor, index to build the mesh

Value

ngme_operator object

`make_time_series_cv_index`*Create Time Series Cross-Validation Indices*

Description

Creates indices for time series cross-validation with options for expanding window or sliding window approaches. Supports both single-step and multi-step forecasting, and can handle replicated observations.

Usage

```
make_time_series_cv_index(  
  time_idx,  
  train_length = NULL,  
  test_length = 1,  
  replicate = time_idx,  
  gap = 0  
)
```

Arguments

<code>time_idx</code>	A numeric vector of time indices in ascending order
<code>train_length</code>	An integer specifying the fixed length of training sets. If NULL (default), an expanding window approach is used.
<code>test_length</code>	An integer specifying the number of observations to include in each test set. Default is 1 (single-step forecasting).
<code>replicate</code>	An optional vector of the same length as <code>time_idx</code> , indicating which observations belong to the same replicate group. When provided, ensures that all observations with the same replicate value are either entirely in the training set or entirely in the test set.
<code>gap</code>	An integer specifying the gap between the training set and test set. Default is 0 (no gap, test set starts immediately after training set). For example, <code>gap=1</code> means skip one time point between training and test (useful for 2-step ahead forecasting).

Details

Time series cross-validation requires respecting the temporal order of observations. This function implements two common approaches:

1. Expanding window (when `train_length = NULL`): The training set grows with each fold, starting with a minimal set and expanding to include all but the test data.
2. Sliding window (when `train_length` is specified): Uses a fixed-length window that slides through the time series, maintaining the same training size across folds.

The `test_length` parameter allows for multi-step forecasting evaluation.

When `replicate` is provided, the function ensures that all observations with the same replicate value are kept together, either all in the training set or all in the test set. This is useful for scenarios where multiple observations at the same time point should be treated as a group.

The `gap` parameter creates a separation between training and test sets, which is useful for multi-step ahead forecasting validation.

Value

A list with two components:

train A list of numeric vectors, where each vector contains the time indices for training in that fold

test A list of numeric vectors, where each vector contains the time indices for testing in that fold

Examples

```
# Expanding window approach with single-step forecasting
cv_expanding <- make_time_series_cv_index(1:10)

# Sliding window approach with window size 3 and single-step forecasting
cv_sliding <- make_time_series_cv_index(1:10, train_length = 3)

# Sliding window with multi-step forecasting (predict 2 steps ahead)
cv_multistep <- make_time_series_cv_index(1:10, train_length = 3, test_length = 2)

# Working with replicates
time_idx <- c(1, 1, 1, 2, 2, 3, 3)
replicates <- c(1, 1, 1, 2, 2, 3, 3)
cv_with_replicates <- make_time_series_cv_index(time_idx, replicate = replicates)

# 2-step ahead forecasting with a gap
cv_with_gap <- make_time_series_cv_index(1:10, gap = 1)
```

matern

ngme Matern SPDE model specification

Description

ngme Matern SPDE model specification

Usage

```
matern(
  mesh = NULL,
  alpha = 2,
  fix_alpha = TRUE,
  kappa = NULL,
  theta_kappa = NULL,
```

```

    rational_order = 2,
    B_kappa = NULL
  )

```

Arguments

mesh	an <code>fmesher::fm_mesh_2d</code> object, mesh for build the SPDE model
alpha	SPDE smoothness parameter ($\alpha = 2\beta$) 2 or 4 for integer case, otherwise for fractional case
fix_alpha	if FALSE, enable fractional modeling
kappa	the range parameter, for the stationary model, it is the range parameter
theta_kappa	$\kappa = \exp(B_kappa * \theta_kappa)$, for the non-stationary model, it is the range parameter
rational_order	order of rational approximation for fractional operators (default: 2)
B_kappa	bases for <code>theta_kappa</code> , ignore if use the stationary model

Value

ngme_operator object

mean_list	<i>taking mean over a list of nested lists</i>
-----------	--

Description

taking mean over a list of nested lists

Usage

```
mean_list(lls, weights = NULL)
```

Arguments

lls	a list
weights	weights of each list

Value

a list of nested lists

Examples

```

ls <- list(
  list(a = 1, b = 2, t = "nig", ll = list(a = 1, b = 2, w = "ab")),
  list(a = 3, b = 5, t = "nig", ll = list(a = 1, b = 6, w = "ab")),
  list(a = 5, b = 5, t = "nig", ll = list(a = 4, b = 2, w = "ab"))
)
mean_list(ls)

```

merge_noise	<i>Merge 2 noise into 1 noise</i>
-------------	-----------------------------------

Description

Merge 2 noise into 1 noise

Usage

```
merge_noise(noise1, noise2)
```

Arguments

noise1	noise 1
noise2	noise 2

Value

merged noise

merge_replicates	<i>Merge model of replicates into model of 1 replicate given train_idx and test_idx, the merged model contains all the information of train_idx from different replicates.</i>
------------------	--

Description

Merge model of replicates into model of 1 replicate given train_idx and test_idx, the merged model contains all the information of train_idx from different replicates.

Usage

```
merge_replicates(ngme, train_idx, test_idx)
```

Arguments

ngme	a ngme object
train_idx	a vector of indices of train data
test_idx	a vector of indices of test data

momentum	<i>Momentum SGD optimization</i>
----------	----------------------------------

Description

Momentum SGD optimization

Usage

```
momentum(stepsize = 0.05, beta1 = 0.9, beta2 = 1 - beta1)
```

Arguments

stepsize	stepsize for SGD
beta1	beta1 for momentum
beta2	beta2 for momentum

Details

The update rule for momentum is:

$$v_t = \beta_1 v_{t-1} + \beta_2 g_t$$

$$x_{t+1} = x_t - \text{stepsize} * v_t$$

Value

a list of control variables for optimization (used in `control_opt` function)

name2fun	<i>Convert transformation name to function</i>
----------	--

Description

This function converts a transformation name to the corresponding function. Conversion is from original scale to real scale by default. Available transformations:

- `exp4`: $\exp(4x)$, inverse is $\log(x)/4$
- `exp2`: $\exp(2x)$, inverse is $\log(x)/2$
- `tanh`: Hyperbolic tangent transformation used for AR1 parameter, uses `ar1_th2a` and `ar1_a2th`
- `identity`: Identity function, no transformation
- `exp`: $\exp(x)$, inverse is $\log(x)$
- `sqrt`: \sqrt{x} , inverse is x^2
- `square`: x^2 , inverse is \sqrt{x}
- `log`: $\log(x)$, inverse is $\exp(x)$

Usage

```
name2fun(trans, inv = FALSE)
```

Arguments

trans	Character string specifying the transformation type from original scale to real scale
inv	Logical, if TRUE returns the transformation function from real scale to original scale

Value

A function that applies the specified transformation

ngme

Fit an additive linear mixed effect model over replicates

Description

ngme function performs an analysis of non-gaussian additive models. It does the maximum likelihood estimation via stochastic gradient descent. The prediction of unknown location can be performed by leaving the response variable to be NA. The likelihood is specified by family. The model estimation control can be setted in control using control_opt() function, see ?control_opt for details. See ngme_model_types() for available models.

Usage

```
ngme(
  formula,
  data,
  family = "normal",
  control_opt = NULL,
  control_ngme = NULL,
  group = NULL,
  replicate = NULL,
  start = NULL,
  moving_window = 1,
  prior_beta = NULL,
  debug = FALSE
)
```

Arguments

formula	formula
data	a dataframe or a list providing data (Only response variable can contain NA value, NA value in other columns will cause problem)

family	likelihood type, same as measurement noise specification. It can be provided as: <ol style="list-style-type: none"> 1. a string, e.g., "normal", "nig", "t". 2. an ngme noise object, e.g., noise_normal(), noise_nig(mu = 0, sigma = 1, nu = 1), noise_t(nu=5).
control_opt	control for optimizer. by default it is control_opt(). See ?control_opt for details.
control_ngme	control for ngme model. by default it is control_ngme(). See ?control_ngme for details.
group	factor, used for bivariate model, indicating which group the observation belongs to
replicate	factor, used for divide data into different replicates
start	starting ngme object (usually object from last fit)
moving_window	number of iterations to average the estimation
prior_beta	prior specification for fixed effects ('beta'), created by prior_*() or priors(...).
debug	toggle debug mode

Value

random effects (for different replicate) + models(fixed effects, measurement noise, and latent process)

Examples

```
ngme(
  formula = Y ~ x1 + f(
    x2,
    model = ar1(rho = 0.5),
    noise = noise_nig()
  ) + f(x1,
    model = rw1(),
    noise = noise_normal(),
  ),
  family = noise_normal(sd = 0.5),
  data = data.frame(Y = 1:5, x1 = 2:6, x2 = 3:7),
  control_opt = control_opt(
    estimation = FALSE
  )
)
```

ngme_as_sparse

Convert sparse matrix into sparse dgCMatrix

Description

Convert sparse matrix into sparse dgCMatrix

Usage

```
ngme_as_sparse(G)
```

Arguments

G matrix

Value

sparse dgCMatrix

ngme_batch_ci	<i>Batch-Means Confidence Intervals from an ngme Fit</i>
---------------	--

Description

Compute Xi-style batch-means confidence intervals directly from trajectories stored in an ‘ngme’ object.

Usage

```
ngme_batch_ci(
  ngme,
  name = "all",
  level = 0.95,
  alpha = 0.501,
  M = NULL,
  N = NULL,
  apply_transform = TRUE,
  drop_burnin = TRUE,
  burnin_iter = 0
)
```

Arguments

ngme	fitted ‘ngme’ object with ‘store_traj = TRUE’ during optimization.
name	either ‘“all”’ (default) to use all parameters jointly, a latent model name, or ‘“general”’ for measurement-noise/fixed-effect block.
level	confidence level.
alpha	stepsize decay exponent in $(1/2, 1)$.
M	number of retained batches (excluding burn-in batch 0).
N	decorrelation constant in the batch boundary formula.
apply_transform	logical; if ‘TRUE’, inference is first computed in the raw optimization space and then mapped to user scale via post-hoc Delta method (Post-delta).

drop_burnin	logical; if 'TRUE', discard batch 0.
burnin_iter	non-negative integer. Explicitly discard the first 'burnin_iter' optimization iterations before Xi-style batching.

Value

Same structure as [batch_means_ci()] with extra metadata fields 'name' and 'apply_transform'.

ngme_cov_matrix	<i>variance of the data or the latent field</i>
-----------------	---

Description

Compute the variance of the data or the latent field

Usage

```
ngme_cov_matrix(ngme_object, model_name = "data", replicate = 1)
```

Arguments

ngme_object	ngme_model
model_name	if model_name = "data", then return the covariance matrix of the data (without measurement noise) if the model_name is the name or index of the latent, then return the covariance matrix of the latent field
replicate	which replicate (default = 1)

Value

a data.frame of posterior samples (mesh_size * n_post_samples)

ngme_make_mesh_repls	<i>ngme make mesh for different replicates</i>
----------------------	--

Description

Make different mesh for different replicates

Usage

```
ngme_make_mesh_repls(data, map, replicate, mesh_type = "regular")
```

Arguments

data	provide the data.frame
map	provide the map to make mesh, i.g. ~x+y, x and y will be extracted from data to make a 2d mesh
replicate	provide the replicate information, i.g. ~id
mesh_type	type of mesh, "regular" means use all the point from same replicate to make a mesh

Value

a list of mesh of length of different replicates

ngme_model_types	<i>Show ngme model types</i>
------------------	------------------------------

Description

Show ngme model types

Usage

```
ngme_model_types()
```

Value

available types for models

ngme_noise	<i>ngme noise specification</i>
------------	---------------------------------

Description

Function for specifying ngme noise. Please use noise_nig and noise_normal for simpler usage. Use ngme_noise_types() to check all the available types.

Usage

```
ngme_noise(  
  noise_type,  
  mu = 0,  
  sigma = 1,  
  nu = 1,  
  B_mu = NULL,  
  theta_mu = NULL,  
  B_sigma = NULL,  
  theta_sigma = NULL,  
  B_nu = NULL,  
  theta_nu = NULL,  
  theta_sigma_normal = NULL,  
  B_sigma_normal = NULL,  
  fix_theta_mu = FALSE,  
  fix_theta_sigma = FALSE,  
  fix_rho = FALSE,  
  fix_theta_sigma_normal = FALSE,  
  fix_theta_nu = FALSE,  
  V = NULL,  
  fix_V = FALSE,  
  single_V = FALSE,  
  share_V = FALSE,  
  corr_measurement = FALSE,  
  index_corr = NULL,  
  map_corr = NULL,  
  nu_lower_bound = 0,  
  rho = double(0),  
  prior = NULL,  
  ...  
)  
  
noise_normal(  
  sigma = NULL,  
  theta_sigma = NULL,  
  B_sigma = matrix(1),  
  corr_measurement = FALSE,  
  index_corr = NULL,  
  ...  
)  
  
noise_nig(  
  mu = NULL,  
  sigma = NULL,  
  nu = NULL,  
  V = NULL,  
  theta_mu = NULL,  
  theta_sigma = NULL,
```

```
    theta_nu = NULL,  
    nu_lower_bound = 0,  
    B_mu = matrix(1),  
    B_sigma = matrix(1),  
    B_nu = matrix(1),  
    corr_measurement = FALSE,  
    index_corr = NULL,  
    ...  
)  
  
noise_gal(  
  mu = NULL,  
  sigma = NULL,  
  nu = NULL,  
  V = NULL,  
  theta_mu = NULL,  
  theta_sigma = NULL,  
  theta_nu = NULL,  
  nu_lower_bound = 0.01,  
  B_mu = matrix(1),  
  B_sigma = matrix(1),  
  B_nu = matrix(1),  
  corr_measurement = FALSE,  
  index_corr = NULL,  
  ...  
)  
  
noise_skew_t(  
  mu = NULL,  
  sigma = NULL,  
  nu = NULL,  
  theta_mu = NULL,  
  theta_sigma = NULL,  
  theta_nu = NULL,  
  nu_lower_bound = 0.01,  
  B_mu = matrix(1),  
  B_sigma = matrix(1),  
  B_nu = matrix(1),  
  corr_measurement = FALSE,  
  index_corr = NULL,  
  ...  
)  
  
noise_t(  
  nu = NULL,  
  theta_nu = NULL,  
  nu_lower_bound = 0,  
  B_nu = matrix(1),
```

```

    corr_measurement = FALSE,
    index_corr = NULL,
    ...
)

noise_normal_nig(
  sigma_normal = NULL,
  mu = NULL,
  sigma_nig = NULL,
  nu = NULL,
  V = NULL,
  theta_mu = NULL,
  theta_sigma_nig = NULL,
  theta_sigma_normal = NULL,
  theta_nu = NULL,
  B_mu = matrix(1),
  B_sigma_nig = matrix(1),
  B_sigma_normal = matrix(1),
  B_nu = matrix(1),
  corr_measurement = FALSE,
  index_corr = NULL,
  ...
)

```

Arguments

noise_type	type of noise, "normal", "nig", "gal", "t", "skew_t"
mu	specify the NIG noise parameter mu, see ?nig
sigma	specify the noise parameter sigma, see ?nig
nu	specify the noise parameter nu, see ?nig and ?gal
B_mu	Basis matrix for mu (if non-stationary)
theta_mu	specify a non-stationary noise using theta_mu
B_sigma	Basis matrix for sigma (if non-stationary)
theta_sigma	specify a non-stationary noise using theta_sigma
B_nu	Basis matrix for nu (if non-stationary)
theta_nu	specify a non-stationary noise using theta_nu
theta_sigma_normal	for normal noise with nig noise sharing same parameter
B_sigma_normal	for normal noise with nig noise sharing same parameter
fix_theta_mu	fix the parameter of theta_mu
fix_theta_sigma	fix the parameter of theta_sigma, can be a single logical value or a vector of logical values with length equal to length(theta_sigma)
fix_rho	fix the parameter of rho

<code>fix_theta_sigma_normal</code>	fix the parameter of <code>sigma_normal</code> , used in <code>noise_normal_nig()</code>
<code>fix_theta_nu</code>	fix the parameter of <code>nu</code>
<code>V</code>	start value for <code>V</code>
<code>fix_V</code>	fix the sampling of <code>V</code> gives $Y W \sim N(\text{mean} * \text{sigma}, \text{sigma}^2)$
<code>single_V</code>	TRUE if <code>V</code> is a single number
<code>share_V</code>	used only for bivariate model
<code>corr_measurement</code>	TRUE if we use correlated measurement noise
<code>index_corr</code>	used when <code>corr_measurement=TRUE</code> , indicate which observation has correlation
<code>map_corr</code>	1d, 2d, or formula, used when <code>corr_measurement=TRUE</code> , specify use which covariate to infer the <code>index_corr</code> .
<code>nu_lower_bound</code>	specify the lower bound of parameter <code>nu</code> ; effective parametrization is $\nu = \nu_{lower_bound} + \exp(B_\nu \theta_\nu)$ so <code>theta_nu</code> remains unconstrained. Default 0.
<code>rho</code>	used when <code>corr_measurement=TRUE</code> , starting point for correlation
<code>prior</code>	prior specification created by <code>priors(...)</code> . Supported keys are <code>mu</code> , <code>sigma</code> , and <code>nu</code> .
<code>...</code>	additional arguments
<code>sigma_normal</code>	for normal noise with <code>nig</code> noise sharing same parameter
<code>sigma_nig</code>	similar to <code>sigma_normal</code>
<code>theta_sigma_nig</code>	similar to <code>theta_sigma_normal</code>
<code>B_sigma_nig</code>	similar to <code>B_sigma_nig</code>

Details

The parameterization is given in `?nig` and `?gal`. Moreover, for specifying non-stationary `mu` and `sigma`, `nu`

$$\mu = B_\mu \theta_\mu,$$

and

$$\sigma = \exp(B_\sigma \theta_\sigma),$$

$$\nu = \nu_{lower} + \exp(B_\nu \theta_\nu).$$

Value

a list of specification of noise

Examples

```
noise_normal(sigma = 2)
noise_nig(mu = 1, sigma = 2, nu = 1)
noise_gal(mu = 1, sigma = 2, nu = 1)
noise_skew_t(mu = 0, sigma = 1, nu = 5)
noise_t(nu = 5)
```

ngme_noise_types	<i>Show ngme noise types</i>
------------------	------------------------------

Description

Show ngme noise types

Usage

```
ngme_noise_types()
```

Value

available types for noise

ngme_optimizers	<i>List supported optimizers</i>
-----------------	----------------------------------

Description

This function returns a list of supported optimizers in the ngme package. The optimizers are categorized into three groups:

- **Gradient descent:** "sgd", "sgld", "momentum", "adaptive_gd"
- **Adaptive learning rate:** "adagrad", "rmsprop", "adam", "adamW"
- **Preconditioner:** "precond_sgd", "bfgs"

Usage

```
ngme_optimizers()
```

Value

a character vector of supported optimizers

ngme_parse_formula *Parse the formula for ngme function*

Description

Parse the formula for ngme function

Usage

```
ngme_parse_formula(  
  fm,  
  data,  
  control_ngme,  
  noise,  
  group,  
  replicate,  
  prior_beta,  
  standardize  
)
```

Arguments

fm	formula
data	data.frame
control_ngme	control_ngme
noise	noise
group	group factor
replicate	replicate vector
prior_beta	prior specification for fixed effects
standardize	logical, whether fixed effects are standardized

Value

a list (replicate) of ngme_replicate models

ngme_post_samples	<i>posterior samples of different latent models</i>
-------------------	---

Description

Extract the posterior samples of different latent models

Usage

```
ngme_post_samples(ngme_object, model_name = 1, type = "W", replicate = 1)
```

Arguments

ngme_object	ngme object
model_name	name of the model, or index of the model
type	type of samples, "W" or "V"
replicate	which replicate

Value

a data.frame of posterior samples (mesh_size * n_post_samples)

ngme_prior_types	<i>Show ngme priors</i>
------------------	-------------------------

Description

Show ngme priors

Usage

```
ngme_prior_types()
```

Value

available types of priors

ngme_result	<i>Access the result of a ngme fitted model</i>
-------------	---

Description

Access the result of a ngme fitted model

Usage

```
ngme_result(ngme_object, model = NULL, transformed = TRUE)
```

Arguments

ngme_object	a ngme fitted model object
model	latent model name to filter by (e.g., "my_ar1", "my_matern", "my_rw1", etc.), "data" for fixed effects and measurement noise, if NULL, return all models
transformed	logical, if TRUE (default) return transformed parameters, if FALSE return raw parameters

Value

a list of parameters for the specified model, or all models if model is NULL

Examples

```
# Fit a simple AR(1) model
set.seed(1)
Y <- 1:10
n_obs <- length(Y)
x1 <- rnorm(n_obs)
x2 <- runif(n_obs)

ngme_out <- ngme(
  Y ~ x1 + x2 + f(
    1:n_obs,
    name = "my_ar",
    model = ar1(rho = 0.5),
    noise = noise_nig(mu = 2, sigma = 3, nu = 1)
  ),
  data = data.frame(x1 = x1, x2 = x2, Y = Y),
  control_opt = control_opt(estimation = FALSE)
)

# Get all model parameters (transformed)
all_params <- ngme_result(ngme_out)
# Returns: list(my_ar = list(rho = 0.5, mu = 2, sigma = 3, nu = 1),
#             data = list(fixed_effects = c(...), sigma = 0.5))

# Get parameters for specific latent model
```

```

ar_params <- ngme_result(ngme_out, model = "my_ar")
# Returns: list(rho = 0.5, mu = 2, sigma = 3, nu = 1)

# Get raw (untransformed) parameters
ar_raw <- ngme_result(ngme_out, model = "my_ar", transformed = FALSE)
# Returns: list(theta_rho = 1.099, mu = 2, sigma = 3, nu = 1)

# Get fixed effects and measurement noise
data_params <- ngme_result(ngme_out, model = "data")
# Returns: list(fixed_effects = c(...), sigma = 0.5, ...)

# For models with multiple latent processes
ngme_out2 <- ngme(
  Y ~ x1 + x2 + f(
    1:n_obs,
    name = "my_ar",
    model = ar1(rho = 0.5),
    noise = noise_nig(mu = 2, sigma = 3, nu = 1)
  ) + f(
    1:n_obs,
    name = "my_ou",
    model = ou(),
    noise = noise_normal(sigma = 1)
  ),
  data = data.frame(x1 = x1, x2 = x2, Y = Y),
  control_opt = control_opt(estimation = FALSE)
)

# Get all models
all_models <- ngme_result(ngme_out2)
# Returns: list(my_ar = list(...), my_ou = list(...), data = list(...))

# Get specific model
ou_params <- ngme_result(ngme_out2, model = "my_ou")
# Returns: list(theta_K1 = 0.5, sigma = 1)

```

ngme_sgld_ci

Quantile Confidence Intervals from SGLD Samples

Description

Compute parameter-wise quantile confidence intervals from posterior-like SGLD samples returned by [ngme_sgld_samples()].

Usage

```
ngme_sgld_ci(samples, lower = 0.025, upper = 0.975)
```

Arguments

samples	data.frame (or list of data.frames) returned by [ngme_sgld_samples()].
lower	lower quantile probability (e.g. 0.025).
upper	upper quantile probability (e.g. 0.975).

Value

A list with posterior-like point estimates ('estimates'), quantile intervals ('ci'), and sample covariance matrix ('covariance'). Class: 'ngme_sgld_ci'.

ngme_sgld_samples	<i>Extract Posterior-like Samples from Stored SGLD Trajectories</i>
-------------------	---

Description

Build posterior-like samples from optimizer trajectories by dropping an initial burn-in segment and applying thinning.

Usage

```
ngme_sgld_samples(
  ngme,
  name = "all",
  burnin_iter = 0,
  thinning = 1,
  apply_transform = TRUE,
  combine_chains = TRUE
)
```

Arguments

ngme	fitted 'ngme' object with 'store_traj = TRUE'.
name	parameter block to extract: "all" (default), latent model name, or "general".
burnin_iter	non-negative integer. Number of initial iterations to discard before sampling.
thinning	positive integer thinning interval.
apply_transform	logical; apply parameter transforms to user scale.
combine_chains	logical; if 'TRUE', return one combined data.frame, otherwise return one data.frame per chain.

Value

A data.frame (or list of data.frames when 'combine_chains = FALSE') with columns '.chain', '.draw', '.iter', and one column per parameter.

ngme_ts_make_A	<i>Make observation matrix for time series</i>
----------------	--

Description

Make observation matrix for time series

Usage

```
ngme_ts_make_A(loc, replicate = NULL, range = c(min(loc), max(loc)))
```

Arguments

loc	integers (after sorting, no gaps > 1)
replicate	indicating replicate measure at same location
range	range for the mesh by default range=(min(loc), max(loc))

Value

A matrix (length(loc) * length(unique(loc)))

Examples

```
ngme_ts_make_A(c(1, 2, 2), replicate = c(1, 1, 2))
ngme_ts_make_A(c(1, 2, 2), range = c(1, 5))
```

ngme_update	<i>Check whether a newer stable version of ngme2 is available</i>
-------------	---

Description

This function checks the package repository for the latest available ngme2 version. It does not install or update packages.

Usage

```
ngme_update()
```

Value

Invisibly returns a list with the local version, remote version, repository URL, and a logical update_available flag.

Description

Density, distribution function, quantile function and random generation for the normal inverse-Gaussian distribution with parameters ν , μ and σ .

Usage

```
dnig(x, delta, mu, nu, sigma, h = NULL, log = FALSE)
```

```
rnig(n, delta, mu, nu, sigma, h = NULL, seed = 0)
```

```
pnig(q, delta, mu, nu, sigma, h = NULL, lower.tail = TRUE, log.p = FALSE)
```

```
qnig(p, delta, mu, nu, sigma, h = NULL, lower.tail = TRUE, log.p = FALSE)
```

Arguments

<code>x, q</code>	vector of quantiles.
<code>delta</code>	A numeric value for the location parameter.
<code>mu</code>	A numeric value for the shift parameter.
<code>nu</code>	A numeric value for the shape parameter.
<code>sigma</code>	A numeric value for the scaling parameter.
<code>h</code>	A numeric value for the additional parameter, see details.
<code>log, log.p</code>	logical; if TRUE, probabilities/densities p are returned as $\log(p)$.
<code>n</code>	number of observations.
<code>seed</code>	Seed for the random generation.
<code>lower.tail</code>	logical; if TRUE, probabilities are $P[X \leq x]$, otherwise, $P[X > x]$.
<code>p</code>	vector of probabilities.

Details

The normal inverse-Gaussian distribution has density given by

$$f(x; \delta, \mu, \sigma, \nu) = \frac{e^{\nu + \mu(x - \delta)/\sigma^2} \sqrt{\nu \mu^2 / \sigma^2 + \nu^2}}{\pi \sqrt{\nu \sigma^2 + (x - \delta)^2}} K_1(\sqrt{(\nu \sigma^2 + (x - \delta)^2)(\mu^2 / \sigma^4 + \nu / \sigma^2)}),$$

where K_p is modified Bessel function of the second kind of order p , $x > 0$, $\nu > 0$ and $\mu, \delta, \sigma \in \mathbb{R}$. See Barndorff-Nielsen (1977, 1978 and 1997) for further details.

The additional parameter h is used when

$$V \sim IG(\nu, \nu h^2)$$

. By the infinite divisibility,

$$\frac{1}{h}V \sim IG(\nu h, \nu h)$$

. Then

$$\delta + \mu V + \sigma \sqrt{V} Z$$

has the distribution of

$$NIG(\delta = -\mu h, \mu = \mu h, \sigma = \sigma \sqrt{h}, \nu = \nu h).$$

Value

dnig gives the density, pnig gives the distribution function, qnig gives the quantile function, and rnig generates random deviates.

Invalid arguments will result in return value NaN, with a warning.

The length of the result is determined by n for rnig.

References

Barndorff-Nielsen, O. (1977) Exponentially decreasing distributions for the logarithm of particle size. Proceedings of the Royal Society of London.

Series A, Mathematical and Physical Sciences. The Royal Society. 353, 401–409. doi:10.1098/rspa.1977.0041

Barndorff-Nielsen, O. (1978) Hyperbolic Distributions and Distributions on Hyperbolae, Scandinavian Journal of Statistics. 5, 151–157.

Barndorff-Nielsen, O. (1997) Normal Inverse Gaussian Distributions and Stochastic Volatility Modelling, Scandinavian Journal of Statistics. 24, 1-13. doi:10.1111/14679469.00045

See Also

[dgig](#), [dig](#), [digam](#)

Examples

```
rnig(100, delta = 0, mu = 5, sigma = 1, nu = 1)
pnig(0.4, delta = 0, mu = 5, sigma = 1, nu = 1)
qnig(0.8, delta = 0, mu = 5, sigma = 1, nu = 1)
plot(function(x){dnig(x, delta = 0, mu = 5, sigma = 1, nu = 1)}, main =
"Normal inverse-Gaussian density", ylab = "Probability density",
xlim = c(0,10))
```

noise_moments	<i>Moments of stationary NIG and GAL noise</i>
---------------	--

Description

Compute the mean, variance, skewness, kurtosis, and excess kurtosis for stationary NIG and GAL noise. The distribution is evaluated through the normal mean-variance mixture

$$X = \delta + \mu V + \sigma \sqrt{V} Z,$$

where $Z \sim N(0, 1)$. For the package's stationary noise parameterization, $\delta = -\mu$, so the mean is zero.

Usage

```
noise_moments(noise, ...)

## S3 method for class 'ngme_noise'
noise_moments(noise, ...)

noise_nig_moments(delta = -mu, mu = 0, sigma = 1, nu = 1)

noise_gal_moments(delta = -mu, mu = 0, sigma = 1, nu = 1)
```

Arguments

noise	An ngme_noise object created by noise_nig() or noise_gal().
...	Currently unused.
delta	Location parameter. Defaults to -mu, matching the stationary ngme noise convention.
mu	Shift/skewness parameter in the mixture mean.
sigma	Positive Gaussian scale parameter.
nu	Positive mixing-distribution shape parameter.

Value

A named numeric vector with entries skewness, kurtosis, excess_kurtosis, variance, sd, central_moment3, and central_moment4.

Examples

```
noise_nig_moments(mu = 1, sigma = 2, nu = 3)
noise_gal_moments(mu = 1, sigma = 2, nu = 3)
noise_moments(noise_nig(mu = 1, sigma = 2, nu = 3))
```

openmp_test	<i>Test OpenMP availability and report the number of threads.</i>
-------------	---

Description

This function checks if OpenMP is available in the current R environment and, if so, reports the number of OpenMP threads detected. If OpenMP is not available, it reports a corresponding message. It relies on an internal or external function ‘get_openmp_threads()’ which is assumed to return the number of threads or 0 if unavailable.

Usage

```
openmp_test()
```

Value

Invisibly returns the detected number of OpenMP threads. A value of zero means OpenMP is not available.

ou	<i>Ornstein-Uhlenbeck Process Model</i>
----	---

Description

Implements the exact discrete-time representation of the continuous Ornstein-Uhlenbeck (OU) process using a matrix formulation $\mathbf{KX} = \delta$.

Usage

```
ou(mesh = NULL, theta = 1)
```

Arguments

mesh	numerical vector or ‘inla.mesh.1d’ object giving the ordered time locations. Must be strictly increasing.
theta	positive mean-reversion rate (stiffness parameter). Internally stored on the log scale so optimization remains unconstrained.

Details

The OU process is defined by the stochastic differential equation (SDE):

$$dX_t = -\theta X_t dt + \sigma dW_t$$

where $\theta > 0$ is the mean-reversion rate (stiffness) and σ is the volatility (diffusion coefficient).

Exact Discretization

Unlike Euler-Maruyama approximations, the OU process has an exact solution between time points t_i and t_{i+1} with step size Δt_i :

$$X_{i+1} = X_i e^{-\theta \Delta t_i} + \epsilon_i$$

This is an AR(1) form with autoregressive coefficient:

$$\rho_i = e^{-\theta \Delta t_i}$$

and Gaussian noise:

$$\epsilon_i \sim \mathcal{N}\left(0, \frac{\sigma^2}{2\theta}(1 - \rho_i^2)\right)$$

Matrix Representation

The precision matrix \mathbf{K} for the linear system $\mathbf{K}\mathbf{X} = \boldsymbol{\delta}$ is constructed as:

$$\mathbf{K} = \begin{bmatrix} \sqrt{1 - \rho_1^2} & 0 & 0 & \cdots & 0 \\ -\rho_1 & 1 & 0 & \cdots & 0 \\ 0 & -\rho_2 & 1 & \cdots & 0 \\ \vdots & \vdots & \ddots & \ddots & \vdots \\ 0 & 0 & \cdots & -\rho_{n-1} & 1 \end{bmatrix}$$

where $\rho_i = \exp(-\theta \Delta t_i)$ with $\Delta t_i = t_{i+1} - t_i$.

****Why the $\sqrt{1 - \rho_1^2}$ term?*** The first row ensures that X_1 is drawn from the stationary distribution $\mathcal{N}(0, \sigma^2/(2\theta))$. This scaling factor matches the variance of the first component of $\boldsymbol{\delta}$ with the transition noise variance in subsequent steps.

Non-uniform Mesh

For non-uniform meshes, each ρ_i is computed locally based on the varying time step Δt_i , allowing the model to naturally handle irregularly spaced observations.

The h vector

The h vector represents integration weights for the mass matrix. For the OU model, it is set as:

$$h = [\Delta t_1, \Delta t_2, \dots, \Delta t_{n-1}, \Delta t_{n-1}]$$

where the last element is duplicated. This ensures proper weighting in the finite element formulation.

The δ vector

In the equation $\mathbf{KX} = \delta$, the vector δ contains independent identically distributed (i.i.d.) random variables with unit variance. The precision matrix \mathbf{K} is constructed such that the resulting process \mathbf{X} has the correct OU covariance structure.

Value

An 'ngme_operator' object containing:

- 'K': the precision matrix
- 'h': integration weights
- 'theta_K': log-transformed theta for unconstrained optimization
- 'mesh': the mesh object

References

Uhlenbeck, G. E., & Ornstein, L. S. (1930). On the theory of the Brownian motion. *Physical review*, 36(5), 823.

Examples

```
# Uniform mesh
mesh_uniform <- seq(0, 10, by = 0.5)
ou_uniform <- ou(mesh = mesh_uniform, theta = 0.5)
print(ou_uniform)

# Non-uniform mesh
mesh_nonuniform <- c(0, 1, 2.5, 3.5, 5, 8, 11)
ou_nonunif <- ou(mesh = mesh_nonuniform, theta = 0.8)
print(ou_nonunif)
```

plot.ngme_noise	<i>Plot the density of one or more stationary noise objects</i>
-----------------	---

Description

This function plots the probability density function for one or more stationary noise objects (e.g., NIG, GAL, or normal noise). Multiple noise objects can be compared on the same plot.

Usage

```
## S3 method for class 'ngme_noise'
plot(x = NULL, ...)
```

Arguments

x	An ngme_noise object (required).
...	Additional ngme_noise objects to plot, or plotting parameters such as xlim. Named arguments will be used as legend labels.

Value

A ggplot object showing the density curves for the provided noise objects.

Examples

```
plot(noise_nig(mu = 1, sigma = 2, nu = 1))
plot(n1 = noise_nig(mu = 0, sigma = 1, nu = 1), n2 = noise_nig(mu = 1, sigma = 1.5, nu = 0.5))
```

```
plot.parameter_distance
```

Plot method for parameter_distance

Description

Plot method for parameter_distance

Usage

```
## S3 method for class 'parameter_distance'
plot(x, ...)
```

Arguments

x	parameter_distance object
...	additional arguments for ggplot

Value

A ggplot object showing the parameter-distance trajectory over optimization iterations. The y-axis is the stored distance $\|theta - \hat{\theta}\|$; plot annotations report the norm and across-chain summary used when x was computed.

```
pm25_quarterly_2022
```

Quarterly PM2.5 monitor averages over CONUS in 2022

Description

A processed example dataset containing quarterly fine particulate matter (PM2.5) averages for monitoring sites in the contiguous United States. The data are derived from the US EPA Air Quality System and AirData pre-generated monitor files and aggregated to site-quarter means.

Usage

```
data("pm25_quarterly_2022")
```

Format

A data frame with 2640 rows and 9 columns.

site_id EPA monitor site identifier.

state State name.

county County name.

lat Monitor latitude in decimal degrees.

lon Monitor longitude in decimal degrees.

quarter Calendar quarter, coded as Q1, Q2, Q3, or Q4.

pm25_q Quarterly average PM2.5 concentration in micrograms per cubic meter.

n_days Number of daily monitor summaries contributing to the quarterly average.

replicate Integer replicate index corresponding to quarter.

Source

US EPA Air Quality System Data Mart and EPA AirData pre-generated files for PM2.5 monitor summaries. <https://www.epa.gov/aqs> https://aqs.epa.gov/aqsweb/airdata/download_files.html

poly_decay

Polynomial schedule helper

Description

Polynomial schedule helper

Usage

```
poly_decay(alpha = 0.501, t0 = 1, burnin_iter = 0)
```

Arguments

alpha polynomial exponent in $(1/2, 1)$.

t0 non-negative schedule offset.

burnin_iter non-negative integer. Initial iterations without polynomial schedule scaling.

Details

Convenience helper that enables polynomial schedule and disables checkpoint-based decay.

Value

a `stepsize_control()` object.

posterior_plot *Plot Posterior Distributions from SGLD Samples*

Description

Visualize marginal posterior distributions of parameters extracted from [ngme_sgld_samples()] or summarized by [ngme_sgld_ci()].

Usage

```
posterior_plot(
  x,
  parameters = NULL,
  type = c("density", "histogram"),
  by_chain = FALSE,
  show_estimate = TRUE,
  show_interval = TRUE,
  lower = NULL,
  upper = NULL,
  bins = 30,
  ncol = NULL,
  ...
)

## S3 method for class 'ngme_sgld_ci'
plot(x, ...)
```

Arguments

x	a data.frame (or list of data.frames) returned by [ngme_sgld_samples()], or an object of class 'ngme_sgld_ci'.
parameters	optional character vector of parameter names to plot. Defaults to all parameter columns.
type	character; "density" (default) or "histogram".
by_chain	logical; if 'TRUE', color distributions by chain when a '.chain' column is available.
show_estimate	logical; add a vertical line at the posterior mean.
show_interval	logical; add vertical lines for the equal-tail interval.
lower	lower quantile probability used for intervals. If 'x' is an 'ngme_sgld_ci' object, the stored value is used by default.
upper	upper quantile probability used for intervals. If 'x' is an 'ngme_sgld_ci' object, the stored value is used by default.
bins	number of bins for histograms.
ncol	number of facet columns. If 'NULL', use 2 columns for multiple parameters and 1 for a single parameter.
...	unused.

Value

A faceted ggplot object.

```
precision_matrix_multivariate
```

Compute the precision matrix for multivariate model

Description

Compute the precision matrix for multivariate model

Usage

```
precision_matrix_multivariate(  
  p,  
  operator_list,  
  rho,  
  theta = NULL,  
  Q = NULL,  
  scale = NULL  
)
```

Arguments

p	dimension, should be integer and greater than 1
operator_list	a list of ngme_operator object (length should be p)
rho	vector with the $p(p-1)/2$ correlation parameters rho_11, rho_21, rho_22, ... rho_p1, rho_p2, ... rho_p(p-1)
theta	parameter for Q matrix (length of 1 when p=2, length of 3 when p=3)
Q	orthogonal matrix of dim p*p (provide when p > 3)
scale	A vector of length p with constants to multiply each operator matrix with

Details

The general model is defined as $\$D \text{diag}(L_{-1}, \dots, L_{-p}) x = M\$$. D is the dependence matrix, it is parameterized by $\$D = Q(\text{theta}) * D_{-l}(\text{cor_mat})\$$, where $\$Q\$$ is the orthogonal matrix, and $\$D_{-l}\$$ is matrix controls the cross-correlation. See the section 2.2 of Bolin and Wallin (2020) for exact parameterization of Dependence matrix.

Value

the precision matrix of the multivariate model

References

Bolin, D. and Wallin, J. (2020), Multivariate type G Matérn stochastic partial differential equation random fields. J. R. Stat. Soc. B, 82: 215-239. <https://doi.org/10.1111/rssb.12351>

Examples

```
rho <- c(-0.5, 0.5, -0.25) # correlation parameters
operator_list <- list(ar1(1:5, rho = 0.4), ar1(1:5, rho = 0.5), ar1(1:5, rho = 0.6))
precision_matrix_multivariate(3, operator_list, rho, theta = c(1, 2, 3))
```

```
precision_matrix_multivariate_spde
```

Compute the precision matrix for multivariate spde Matern model

Description

Compute the precision matrix for multivariate spde Matern model

Usage

```
precision_matrix_multivariate_spde(
  p,
  mesh,
  rho,
  alpha_list = NULL,
  theta_K_list = NULL,
  variance_list = NULL,
  B_K_list = NULL,
  theta = NULL,
  Q = NULL
)
```

Arguments

<code>p</code>	dimension, should be integer and greater than 1
<code>mesh</code>	an <code>fmesher::fm_mesh_2d</code> object, mesh for build the SPDE model
<code>rho</code>	vector with the $p(p-1)/2$ correlation parameters <code>rho_11, rho_21, rho_22, ... rho_p1, rho_p2, ... rho_p(p-1)</code>
<code>alpha_list</code>	a list of SPDE smoothness parameter
<code>theta_K_list</code>	a list (length is <code>p</code>) of <code>theta_K</code>
<code>variance_list</code>	If provided, it should be a vector of length <code>p</code> , where the <code>k</code> th element corresponds to a desired variance of the <code>k</code> th field. The <code>k</code> th operator is then scaled by a constant <code>c</code> so that this variance is achieved in the stationary case (default no scaling)
<code>B_K_list</code>	a list (length is <code>p</code>) of <code>B_K</code> (non-stationary case)
<code>theta</code>	parameter for <code>Q</code> matrix (length of 1 when <code>p=2</code> , length of 3 when <code>p=3</code>)
<code>Q</code>	orthogonal matrix of dim <code>p*p</code> (provide when <code>p > 3</code>)

Details

The general model is defined as $D \text{diag}(L_1, \dots, L_p) x = M$. D is the dependence matrix, it is parameterized by $D = Q(\theta) * D_l(\text{cor_mat})$, where Q is the orthogonal matrix, and D_l is matrix controls the cross-correlation. See the section 2.2 of Bolin and Wallin (2020) for exact parameterization of Dependence matrix.

Value

the precision matrix of the multivariate model

References

Bolin, D. and Wallin, J. (2020), Multivariate type G Matérn stochastic partial differential equation random fields. *J. R. Stat. Soc. B*, 82: 215-239. <https://doi.org/10.1111/rssb.12351>

Examples

```
library(fmesher)

# Use a small mesh so the example stays lightweight.
x <- seq(from = 0, to = 1, length.out = 6)
mesh <- fm_rcdt_2d_inla(lattice = fm_lattice_2d(x, x), extend = FALSE)

Q <- precision_matrix_multivariate_spde(
  p = 2,
  mesh = mesh,
  rho = 0.25,
  alpha_list = list(2, 2),
  theta_K_list = list(0, 0),
  variance_list = list(1, 1)
)
dim(Q)
```

```
precond_sgd
```

```
Preconditioner SGD optimization
```

Description

Preconditioner SGD optimization

Usage

```
precond_sgd(stepsize = 1, numerical_eps = 1e-05)
```

Arguments

stepsize stepsize for SGD
numerical_eps numerical, the gap used for estimate preconditioner, default is 1e-5

Details

Preconditioner SGD is using fisher information matrix as preconditioner (natural gradient descent).

Value

a list of control variables for optimization (used in control_opt function)

predict.ngme	<i>Predict function of ngme2 predict using ngme after estimation</i>
--------------	--

Description

Predict function of ngme2 predict using ngme after estimation

Usage

```
## S3 method for class 'ngme'
predict(
  object,
  map,
  data = NULL,
  type = "lp",
  group = NULL,
  estimator = c("mean", "sd", "0.05q", "0.95q", "median", "mode"),
  sampling_size = 500,
  burnin_size = 100,
  seed = Sys.time(),
  train_idx = NULL,
  chain_combine = c("param_mean", "predictive_average"),
  return_samples = FALSE,
  ...
)
```

Arguments

object	a ngme object
map	a named list (or dataframe) of the locations to make the prediction
data	a data.frame or matrix of covariates (used for fixed effects) names(loc) corresponding to the name each latent model vector or matrix (n * 2) for spatial coords
type	what type of prediction, c("fe", "lp", <model_name>) "fe" is fixed effect prediction <model_name> is prediction of a specific model "lp" is linear predictor (including fixed effect and all sub-models) "response" is the linear predictor plus a fresh measurement-noise draw
group	which filed to predict (used for bivariate model, should be of same length as map)

estimator	what type of estimator. Options include: - "mean", "median", "mode", "sd": standard estimators - "0.XXXq": any quantile specified as probability (e.g., "0.025q", "0.5q", "0.975q")
sampling_size	size of posterior sampling
burnin_size	size of posterior burnin
seed	random seed
train_idx	optional vector of training indices to use for posterior sampling. If provided, only these indices from the original data will be used for training, similar to cross-validation. If NULL, uses all original training data.
chain_combine	how to combine multiple optimization chains: <ul style="list-style-type: none"> • "param_mean": default behavior using the fitted object parameters. • "predictive_average": run prediction for each optimization chain and average predictions across chains.
return_samples	logical; when 'TRUE', attach sample draws for the requested output in 'attr(ret, "samples")'. For 'type = "response"', the attached samples are response predictive draws.
...	additional arguments (currently unused)

Value

a list of outputs contains estimation of operator paramters, noise parameters

print.ngme	<i>Print an ngme model</i>
------------	----------------------------

Description

Print an ngme model

Usage

```
## S3 method for class 'ngme'
print(x, ...)
```

Arguments

x	ngme model object
...	...

Value

Invisibly returns x, an ngme object. The method is called for its side effect of printing a model summary.

print.ngme_model *Print ngme model*

Description

Print ngme model

Usage

```
## S3 method for class 'ngme_model'  
print(x, padding = 0, ...)
```

Arguments

x	ngme model object
padding	number of white space padding in front
...	...

Value

a list (model specifications)

print.ngme_noise *Print ngme noise*

Description

Print ngme noise

Usage

```
## S3 method for class 'ngme_noise'  
print(x, padding = 0, prefix = "Noise type", model_type = NULL, ...)
```

Arguments

x	noise object
padding	number of white space padding in front
prefix	prefix
model_type	model type
...	...

Value

a list (noise specifications)

```
print.ngme_operator Print ngme operator
```

Description

Print ngme operator

Usage

```
## S3 method for class 'ngme_operator'
print(x, padding = 0, prefix = "Model type", ...)
```

Arguments

x	ngme operator object
padding	number of white space padding in front
prefix	prefix string
...	...

Value

a list (operator specifications)

```
print.ngme_replicate Print ngme object
```

Description

Print ngme object

Usage

```
## S3 method for class 'ngme_replicate'
print(x, ...)
```

Arguments

x	ngme object
...	ignored

Value

Invisibly returns x, an ngme_replicate object. The method is called for its side effect of printing a replicate summary.

```
print.ngme_trajectories
```

Print method for ngme_trajectories

Description

Print method for ngme_trajectories

Usage

```
## S3 method for class 'ngme_trajectories'  
print(x, ...)
```

Arguments

x	ngme_trajectories object
...	additional arguments

Value

Invisibly returns x, an ngme_trajectories object. The method is called for its side effect of printing a summary of stored parameter trajectory matrices, including parameter names, chain count, and iteration count.

```
print.noise_kld_comparison
```

Print method for noise_kld_comparison

Description

Print method for noise_kld_comparison

Usage

```
## S3 method for class 'noise_kld_comparison'  
print(x, ...)
```

Arguments

x	noise_kld_comparison object
...	additional arguments

Value

Invisibly returns x, a noise_kld_comparison object. The method is called for its side effect of printing the reference noise object, the Kullback-Leibler divergence values for each comparison noise, and the closest comparison.

```
print.parameter_distance
```

Print method for parameter_distance

Description

Print method for parameter_distance

Usage

```
## S3 method for class 'parameter_distance'  
print(x, ...)
```

Arguments

x	parameter_distance object
...	additional arguments

Value

Invisibly returns x, a numeric vector with class parameter_distance. The method is called for its side effect of printing the norm type, chain summary, number of iterations, final distance, and true parameter values.

```
priors
```

Prior Container

Description

Prior Container

Usage

```
priors(...)
```

Arguments

...	named prior specifications
-----	----------------------------

Value

named prior container

prior_half_cauchy *Prior Half-Cauchy*

Description

Prior Half-Cauchy

Usage

```
prior_half_cauchy(scale = 1, target = "coef")
```

Arguments

scale	half-Cauchy scale
target	apply prior on coefficient scale ("coef") or field scale ("field")

Value

prior specification

prior_inv_exponential *Prior Inverse-Exponential*

Description

Prior induced by $\kappa = 1/\nu \sim \text{Exp}(\lambda)$, giving $p(\nu) = \lambda \exp(-\lambda/\nu)\nu^{-2}$ for $\nu > 0$. Internally this prior is applied to $\nu = \text{lower} + \exp(\theta)$.

Usage

```
prior_inv_exponential(lambda = 1, lower = 0, target = "coef")
```

```
prior_inv_exp(lambda = 1, lower = 0, target = "coef")
```

Arguments

lambda	exponential rate on $\kappa = 1/\nu$
lower	lower shift used in $\nu = \text{lower} + \exp(\theta)$
target	apply prior on coefficient scale ("coef") or field scale ("field")

Value

prior specification

prior_none	<i>Prior None</i>
------------	-------------------

Description

Prior None

Usage

```
prior_none(target = "coef")
```

Arguments

target apply prior on coefficient scale ("coef") or field scale ("field")

Value

prior specification

prior_normal	<i>Prior Normal</i>
--------------	---------------------

Description

Prior Normal

Usage

```
prior_normal(mean = 0, sd = 1, target = "coef")
```

Arguments

mean prior mean
 sd prior standard deviation
 target apply prior on coefficient scale ("coef") or field scale ("field")

Value

prior specification

prior_pc_sd	<i>Prior PC-SD</i>
-------------	--------------------

Description

Prior PC-SD

Usage

```
prior_pc_sd(u, alpha, target = "coef")
```

Arguments

u	tail event threshold
alpha	tail probability
target	apply prior on coefficient scale ("coef") or field scale ("field")

Value

prior specification

re	<i>ngme random effect model</i>
----	---------------------------------

Description

ngme random effect model

Usage

```
re(map, theta_K = NULL, ...)
```

Arguments

map	numerical vector, covariates to build index for the process (can be formula, provided data)
theta_K	initial value for theta_K (build covariance matrix)
...	currently ignored

Value

ngme_operator object

 rmsprop

Root Mean Square Propagation (RMSProp) SGD optimization

Description

Root Mean Square Propagation (RMSProp) SGD optimization

Usage

```
rmsprop(stepsize = 0.05, beta1 = 0.9, epsilon = 1e-08)
```

Arguments

stepsize	stepsize for SGD
beta1	beta1 for momentum
epsilon	epsilon for numerical stability

Details

The update rule for RMSProp is:

$$v_t = \beta_1 v_{t-1} + (1 - \beta_1) g_t^2$$

$$x_{t+1} = x_t - \text{stepsize} * \frac{g_t}{\sqrt{v_t + \epsilon}}$$

Value

a list of control variables for optimization (used in `control_opt` function)

 rw1

Random Walk Model of Order 1 (RW1)

Description

Constructs a first-order random walk model for spatial or temporal processes. The RW1 model assumes that first-order differences $\Delta W_i = W_i - W_{i-1}$ are independent and identically distributed Gaussian variables.

Usage

```
rw1(mesh = NULL, cyclic = FALSE, constr = TRUE)
```

Arguments

mesh	numerical vector or <code>inla.mesh.1d</code> object, locations to build the mesh. For numerical vectors, assumes equally spaced locations.
cyclic	logical, whether the mesh is circular. If TRUE, the first and last locations are treated as neighbors. Cannot be FALSE when <code>constr = TRUE</code> .
constr	logical, whether to enforce the sum-to-zero constraint $\sum_{i=1}^n h_i W_i = 0$. If FALSE, fixes the first element $W_1 = 0$. Must be TRUE for cyclic models.

Details

The RW1 model is defined by the precision matrix K that penalizes first-order differences. The model has different structures depending on the constraints:

****Non-cyclic, constrained (default)**:** The first row of K enforces the constraint $\sum_{i=1}^n h_i W_i = 0$, where h_i are the mesh weights.

****Non-cyclic, unconstrained**:** The first element is fixed at 0 ($W_1 = 0$).

****Cyclic**:** Treats the domain as circular, connecting the first and last locations as neighbors. The constraint $\sum_{i=1}^n h_i W_i = 0$ is always enforced. The precision matrix is expanded to size $(n + 1) \times (n + 1)$ to handle the constraint properly.

Value

An `'ngme_operator'` object containing the precision matrix and related components for the RW1 model.

Examples

```
# Non-cyclic constrained RW1 (default)
rw1_default <- rw1(1:5)
print(rw1_default$K)

# Non-cyclic unconstrained RW1 (fixes first element to 0)
rw1_fixed <- rw1(1:5, constr = FALSE)
print(rw1_fixed$K)

# Cyclic RW1 (connects first and last locations)
rw1_cyclic <- rw1(1:5, cyclic = TRUE)
print(rw1_cyclic$K)

# Using with unequally spaced locations
locations <- c(0, 1, 3, 6, 10)
rw1_unequal <- rw1(locations)
print(rw1_unequal$K)
```

rw2

*Random Walk Model of Order 2 (RW2)***Description**

Constructs a second-order random walk model for spatial or temporal processes. The RW2 model assumes that second-order differences $\Delta^2 W_i = W_i - 2W_{i-1} + W_{i-2}$ are independent and identically distributed Gaussian variables.

Usage

```
rw2(mesh = NULL, cyclic = FALSE, constr = TRUE)
```

Arguments

mesh	numerical vector or <code>inla.mesh.1d</code> object, locations to build the mesh. For numerical vectors, assumes equally spaced locations. Must have at least 3 locations.
cyclic	logical, whether the mesh is circular. If TRUE, the first and last locations are treated as neighbors with second-order differences computed across the boundary.
constr	logical, whether to enforce the sum-to-zero constraint $\sum_{i=1}^n h_i W_i = 0$ and the linear trend constraint $\sum_{i=1}^n (\sum_{j=1}^i h_j - h_1) \cdot W_i = 0$. If FALSE, fixes the first and second elements $W_1 = 0$ and $W_2 = 0$.

Details

The RW2 model is defined by the precision matrix K that penalizes second-order differences, making it smoother than RW1. The model enforces constraints to ensure identifiability:

****Non-cyclic (default)**:** The first two rows of K enforce constraints: the first row implements $\sum_{i=1}^n h_i W_i = 0$ (sum-to-zero), and the second row implements $\sum_{i=1}^n h_i \cdot i \cdot W_i = 0$ (removes linear trend). The remaining rows penalize second-order differences.

****Cyclic**:** Treats the domain as circular, connecting the first and last locations as neighbors. The constraint $\sum_{i=1}^n h_i W_i = 0$ is enforced. The precision matrix is expanded to size $(n + 1) \times (n + 1)$ to handle the constraint and circular structure properly.

Value

An ‘ngme_operator’ object containing the precision matrix and related components for the RW2 model.

Examples

```
# Non-cyclic RW2 with constraints (default)
rw2_default <- rw2(1:6)
print(rw2_default$K)

# Cyclic RW2 (connects first and last locations)
```

```
rw2_cyclic <- rw2(1:6, cyclic = TRUE)
print(rw2_cyclic$K)

# Using with unequally spaced locations
locations <- c(0, 1, 3, 6, 10, 15)
rw2_unequal <- rw2(locations)
print(rw2_unequal$K)
```

sgd*Vanilla SGD optimization*

Description

Simple stochastic gradient descent without momentum or preconditioning.

Usage

```
sgd(stepsize = 0.001)
```

Arguments

stepsize stepsize for SGD

Value

a list of control variables for optimization (used in `control_opt` function)

sgld*Stochastic Gradient Langevin Dynamics (SGLD) optimization*

Description

Stochastic Gradient Langevin Dynamics (SGLD) optimization

Usage

```
sgld(stepsize = 0.001, temperature = 1)
```

Arguments

stepsize base stepsize
temperature non-negative Langevin temperature

Details

SGLD adds Gaussian noise to vanilla SGD updates:

$$x_{t+1} = x_t - \eta_t \nabla U(x_t) + \sqrt{2T\eta_t} \xi_t, \quad \xi_t \sim \mathcal{N}(0, I)$$

where T is temperature. The implementation applies this component-wise using the current effective stepsize.

Value

a list of control variables for optimization (used in `control_opt` function)

simulate.ngme

Simulate from a ngme object (possibly with replicates)

Description

Simulate from a ngme object (possibly with replicates)

Usage

```
## S3 method for class 'ngme'
simulate(object, nsim = 1, seed = NULL, ...)
```

Arguments

object	ngme object
nsim	number of simulations
seed	seed
...	optional arguments. Supported names are <code>posterior</code> (whether to simulate from posterior sampling of latent fields) and <code>m_noise</code> (whether to add the measurement noise).

Value

a realization of ngme object

simulate.ngme_model *Simulate latent process with noise*

Description

Simulate latent process with noise

Usage

```
## S3 method for class 'ngme_model'  
simulate(object, nsim = 1, seed = NULL, ...)
```

Arguments

object	ngme model specified by f() function
nsim	number of simulations
seed	seed
...	ignored

Value

a realization of latent model

Examples

```
simulate(f(1:10, model = ar1(rho = 0.4), noise = noise_nig()))  
simulate(f(rnorm(10), model = rw1(), noise = noise_normal()))  
simulate(f(1:10, model = ar1(rho = 0.4), noise = noise_t(nu = 5)))
```

simulate.ngme_noise *Simulate ngme noise object*

Description

Simulate ngme noise object

Usage

```
## S3 method for class 'ngme_noise'  
simulate(object, nsim = 1, seed = NULL, h = NULL, ...)
```

Arguments

object	ngme noise object
nsim	number of simulations
seed	seed
h	should be of same length as nsim
...	ignored

Value

data.frame (each col is a realization)

spacetime

Ngme space-time non-separable model specification

Description

Implements a non-separable space-time model based on the advection-diffusion SPDE with first-order derivative in time. The model combines temporal and spatial components through a finite difference method (implicit Euler) for temporal discretization and finite element method (continuous Galerkin) for spatial discretization. When advection dominates diffusion, the "Streamline Diffusion" stabilization technique is applied.

Usage

```
spacetime(
  mesh,
  lambda = 1,
  alpha = 2,
  cc = 1,
  kappa = 1,
  fix_gamma = FALSE,
  theta_gamma_x = 0,
  theta_gamma_y = 0,
  shared_theta_gamma = FALSE,
  B_gamma_x = matrix(1, nrow = mesh[[2]]$n, ncol = 1),
  B_gamma_y = matrix(1, nrow = mesh[[2]]$n, ncol = 1),
  B_gamma_x_list = NULL,
  B_gamma_y_list = NULL,
  stabilization = TRUE
)
```

Arguments

mesh	A list of two objects: <ul style="list-style-type: none"> • mesh_t - The temporal mesh • mesh_s - The spatial mesh
lambda	The spatial damping parameter.
alpha	2 or 4, SPDE smoothness parameter.
cc	Parameter c in the SPDE.
kappa	Kappa parameter from Matern SPDE.
fix_gamma	TRUE if fix gamma (advection term), FALSE if estimate gamma.
theta_gamma_x	The x component of the advection term: $\gamma_x = B_{\gamma_x} \theta_{\gamma_x}$.
theta_gamma_y	The y component of the advection term: $\gamma_y = B_{\gamma_y} \theta_{\gamma_y}$.
shared_theta_gamma	TRUE if share the same theta_gamma for all time nodes. (theta_gamma_x and theta_gamma_y will be the same)
B_gamma_x	The design matrix for the x component of the advection term.
B_gamma_y	The design matrix for the y component of the advection term.
B_gamma_x_list	A list of design matrices for the x component of the advection term on every time node, $\text{length}(B_{\gamma_x_list}) == nt-1$.
B_gamma_y_list	A list of design matrices for the y component of the advection term on every time node, $\text{length}(B_{\gamma_y_list}) == nt-1$.
stabilization	TRUE if using a stabilization term (for implicit Euler).

Details

The model is particularly useful for large space-time datasets in environmental science, offering computationally efficient methods for parameter estimation, kriging prediction, and conditional simulations.

For details, see [doi:10.1016/j.spasta.2024.100847](https://doi.org/10.1016/j.spasta.2024.100847)

Value

ngme_operator object.

stepsize_control	<i>Unified stepsize control</i>
------------------	---------------------------------

Description

Unified stepsize control

Usage

```
stepsize_control(
  schedule = stepsize_schedule(method = "constant"),
  decay = stepsize_decay(method = "none")
)
```

Arguments

schedule	schedule component. Either an object from <code>stepsize_schedule()</code> or a method string accepted by <code>stepsize_schedule()</code> .
decay	decay component. Either an object from <code>stepsize_decay()</code> or a method string accepted by <code>stepsize_decay()</code> .

Details

Bundle an iteration schedule (`stepsize_schedule`) and an optional checkpoint-based decay rule (`stepsize_decay`) into one object for `control_opt()`.

Value

a bundled stepsize-control object for `control_opt()`.

stepsize_decay	<i>Stepsize decay schedule</i>
----------------	--------------------------------

Description

Stepsize decay schedule

Usage

```
stepsize_decay(
  method = c("none", "grad_norm_plateau"),
  patience = 3,
  gamma = 0.5,
  min_delta = 0,
  warmup = 0,
  min_stepsize = 0
)
```

Arguments

method	decay strategy. "none" disables decay; "grad_norm_plateau" decays when mean <code>grad.norm()</code> across chains fails to decrease for a number of epochs.
patience	number of consecutive epochs without <code>grad.norm()</code> improvement before decaying stepsize.

gamma	decay factor applied when triggered ($0 < \text{gamma} < 1$).
min_delta	minimum required decrease in <code>grad.norm()</code> to be counted as improvement.
warmup	number of initial epochs to skip decay checks.
min_stepsize	lower bound for stepsize after decay (absolute value).

Details

Define a stepsize decay strategy for use in `control_opt()`. Currently supports the plateau-based schedule using `grad.norm()`.

Value

a list of control variables for stepsize decay (used in `control_opt()`).

stepsize_schedule	<i>Stepsize schedule</i>
-------------------	--------------------------

Description

Stepsize schedule

Usage

```
stepsize_schedule(
  method = c("constant", "poly"),
  alpha = 0.501,
  t0 = 1,
  burnin_iter = 0
)
```

Arguments

method	schedule type. "constant" keeps $\eta_t = \eta_0$ and "poly" uses polynomial decay.
alpha	polynomial exponent used when method = "poly". Must satisfy $1/2 < \alpha < 1$.
t0	non-negative offset in iteration index.
burnin_iter	non-negative integer. During these initial iterations, schedule scaling is fixed to 1. Afterward, polynomial decay is applied with reset local time index.

Details

Define an iteration-dependent stepsize schedule for use in `control_opt()`. This schedule is independent of `stepsize_decay()` and applies a direct multiplicative scaling by iteration index:

$$\eta_t = \eta_0(t + t_0)^{-\alpha}$$

Value

a list of control variables for stepsize schedule (used in control_opt).

summary.ngme	<i>Summary of ngme fit result</i>
--------------	-----------------------------------

Description

Summary of ngme fit result

Usage

```
## S3 method for class 'ngme'
summary(object, name = NULL, ...)
```

Arguments

object	an object of class ngme
name	name of the latent model to be summarized (if NULL, will print all)
...	other arguments

Value

a list of summary

summary.ngme_batch_ci	<i>Summary for Batch-Means CI Results</i>
-----------------------	---

Description

Summarize an object of class 'ngme_batch_ci', including parameter means, standard errors, confidence intervals, and covariance matrix.

Usage

```
## S3 method for class 'ngme_batch_ci'
summary(object, digits = 4, ...)
```

Arguments

object	an object of class 'ngme_batch_ci'.
digits	number of digits used for printing.
...	currently unused.

Value

A list with summary table and covariance matrix.

tp	<i>ngme tensor-product model specification</i>
----	--

Description

Given 2 operator (first and second), build a tensor-product operator based on $K = K_first \times K_second$ (here \times is Kronecker product)

Usage

```
tp(first, second)
```

Arguments

first	ngme_operator, left side of kronecker model (usually a temporal or iid model)
second	ngme_operator, right side of kronecker model (usually a temporal or spatial model)

Value

a list of specification of model

traceplot	<i>Trace plot of ngme fitting</i>
-----------	-----------------------------------

Description

Trace plot of ngme fitting

Usage

```
traceplot(  
  ngme,  
  name = "all",  
  moving_window = 1,  
  hline = NULL,  
  combine = TRUE,  
  ncol = NULL  
)
```

Arguments

ngme	ngme object
name	name of latent models, otherwise plot fixed effects and measurement noise. Use "all" to plot all latent models plus data parameters in one figure. should be in names(ngme\$models) or other
moving_window	moving window for the traceplot
hline	vector, add hline to each plot
combine	bool, if TRUE, return a single faceted ggplot; otherwise return a list of ggplot objects and print them one by one.
ncol	number of facet columns when combine = TRUE. If NULL (default), use 2 columns for multi-parameter plots and 1 for single-parameter plots.

Value

A ggplot object when combine = TRUE; otherwise a list of ggplot objects. The mean parameter trajectories are stored in the avg_lines attribute of the returned object.

var1	<i>ngme VAR(1) bivariate model specification (Cayley re-parameterization)</i>
------	---

Description

Builds a Vector Autoregressive order-1 (VAR(1)) operator for bivariate time-series data. The model follows:

$$Y_t = A Y_{t-1} + \varepsilon_t, \quad A = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix}$$

Usage

```
var1(mesh = NULL, p1 = 0, p2 = 1, p3 = 0, p4 = 1)
```

Arguments

mesh	Integer vector or <code>inla.mesh.1d</code> object for the time mesh (length T). Pass NULL for deferred construction.
p1	Unconstrained skew-symmetric parameter ($\in \mathbb{R}$); controls the rotation part of the Cayley mapping. Default 0.
p2, p3, p4	Unconstrained lower-triangular Cholesky parameters ($\in \mathbb{R}$); control the contraction (positive-definite) part. Defaults p2 = 1, p3 = 0, p4 = 1.

Value

An `ngme_operator` (or `ngme_operator_def` when mesh = NULL) suitable for use inside `f()`.

Cayley re-parameterization

To guarantee stationarity ($\rho(A) < 1$) at every SGD step, the 2×2 coefficient matrix A is obtained via the *Cayley transform*:

$$A = (I + S)(I - S)^{-1}$$

where S is constructed from four unconstrained real parameters $(p_1, p_2, p_3, p_4) \in \mathbb{R}^4$ as $S = J - R$:

Skew-symmetric part (rotation): $J = \begin{pmatrix} 0 & p_1 \\ -p_1 & 0 \end{pmatrix}$

Positive-definite part (contraction): $R = LL^\top + \varepsilon I$, where $L = \begin{pmatrix} p_2 & 0 \\ p_3 & p_4 \end{pmatrix}$ and $\varepsilon = 10^{-5}$.

Because $S + S^\top = -2R$ is negative definite, all eigenvalues of S have strictly negative real parts, and the Cayley transform then guarantees $|\lambda_i(A)| < 1$ for every i .

The default values $(p_1, p_2, p_3, p_4) = (0, 1, 0, 1)$ give $A \approx 0$ (no auto-regression at initialization).

Precision operator

The 2T x 2T precision operator is:

$$K = M_0 + a_{11} M_{11} + a_{22} M_{22} + a_{12} M_{12} + a_{21} M_{21}$$

where the M_{ij} are fixed sparse block matrices constructed from the $T \times T$ first-order difference matrix C_T .

Examples

```
set.seed(1)
n_obs <- 10
dat <- data.frame(
  y      = rnorm(2 * n_obs),
  idx    = rep(seq_len(n_obs), 2),
  group  = factor(rep(c("y1", "y2"), each = n_obs))
)

fit <- ngme(
  y ~ 0 + f(idx, model = varl(mesh = 1:n_obs), group = group,
    noise = noise_nig()),
  data    = dat,
  family  = noise_normal(sigma = 0.01, fix_sigma = TRUE),
  control_opt = control_opt(estimation = FALSE)
)
print(fit)
```

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